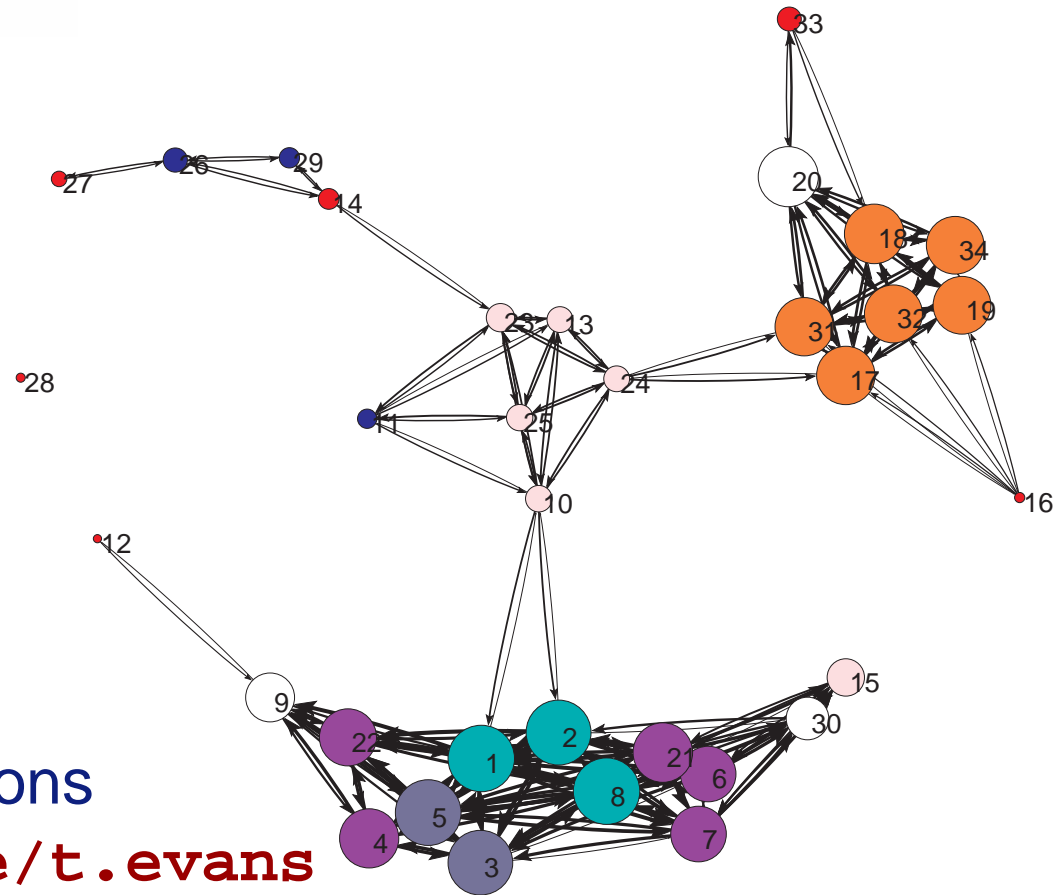


## Networks for the Minoan Aegean

Tim Evans (Imperial),  
Carl Knappett (Exeter),  
Ray Rivers (Imperial)



See web site for publications

[www.ic.ac.uk/people/t.evans](http://www.ic.ac.uk/people/t.evans)

- e.g. see **ISCOM** project *D.Lane et al. (ed.s) 2007*

*“Physical and Relational Networks in the Aegean Bronze Age”*

# 'Minoa'

A reconstruction on show in Chania, Crete



**See commentary on the modern context of this reconstruction**

# Approaches to Modelling

Several approaches when studying settlement patterns, many take *settlements* as the core unit.

- e.g. see EU ISCOM project D.Lane et al. (ed.s) 2007

## Agent Based Modelling

People/Goats as agents e.g. MASS group

Cities as agents e.g. SIMPOP2 (Pumain et al.)

## Network Optimisation

*TSE, CJK, RJR ariadne*

**Equations**  
e.g. West et al.

Increasing Detail

Coarse Graining Increasing

# Site-Site Interactions

- In archaeology relatively little attention has been given to the potential of interactions between sites being involved in the generation of those sites

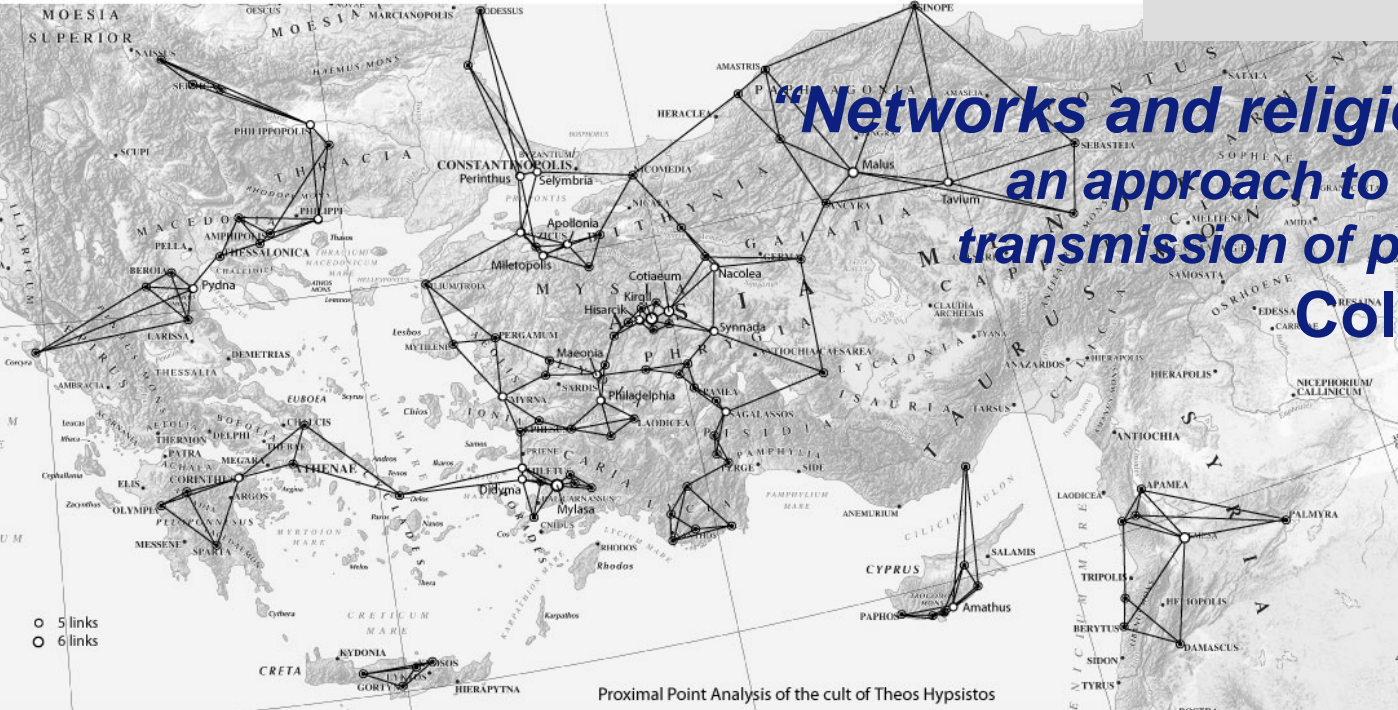
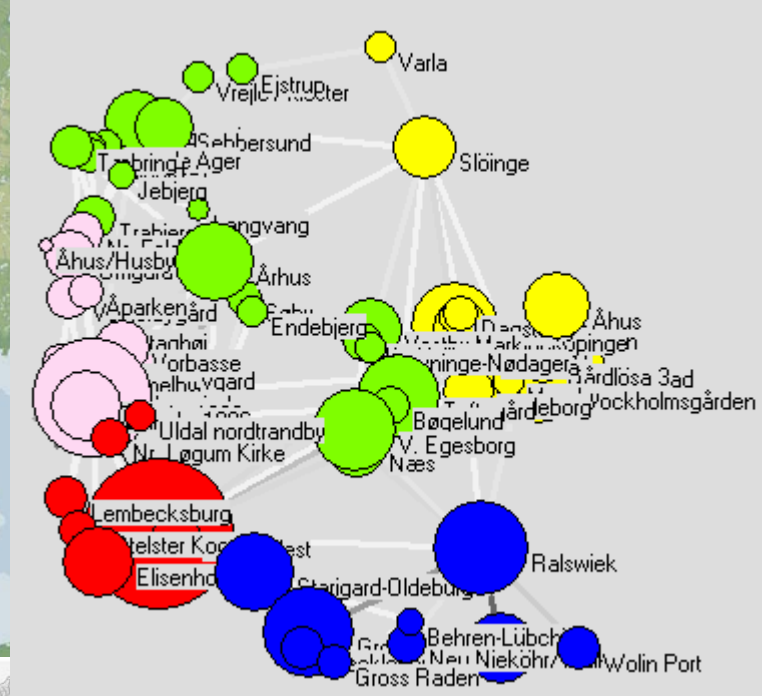
⇒ Network models may prove to be useful

- Most models fixed site sizes, focused on local interactions, often just nearest neighbour interactions

– Malta (*Renfrew & Level, 1979*);  
Geometric Greece (*Rihll & Wilson, 1991*);  
**Proximal Point Analysis** (*Terrell 1977; Irwin 1983;*  
*Hage and Harary, 1991, 1996; Broodbank 2000;*  
*Sindbæk (in prep.); Collar (in prep.)*)



**“The Small World of the Vikings”,  
Sindbæk, Aarhus Univ.  
Anskar’s Vita +  
data from finds,  
9<sup>th</sup> c. AD**



Proximal Point Analysis of the cult of Theos Hypsistos

**“Networks and religious innovation:  
an approach to understanding the  
transmission of pagan monotheism”**

**Collar, Exeter Univ.  
Hypsistos cult  
inscriptions,  
1-4c. AD**

# Island Archipelagos as an Ideal Network

- Vertices = Major Population or Resource Sites
- Edges = Exchange between sites
  - physical trade of goods *or* transmission of culture
  - direct contact *or* island hopping links
- Sea isolates communities → **Natural Vertices**
- Interactions controlled by physical limitations of ancient sea travel → **Simple Links**
- Coastal Sites often isolated like islands due to geography and difficulty of ancient land travel

# Earlier Island Network:- The Kula Ring

Malinowski (1922)

Hage and Harary (1991)

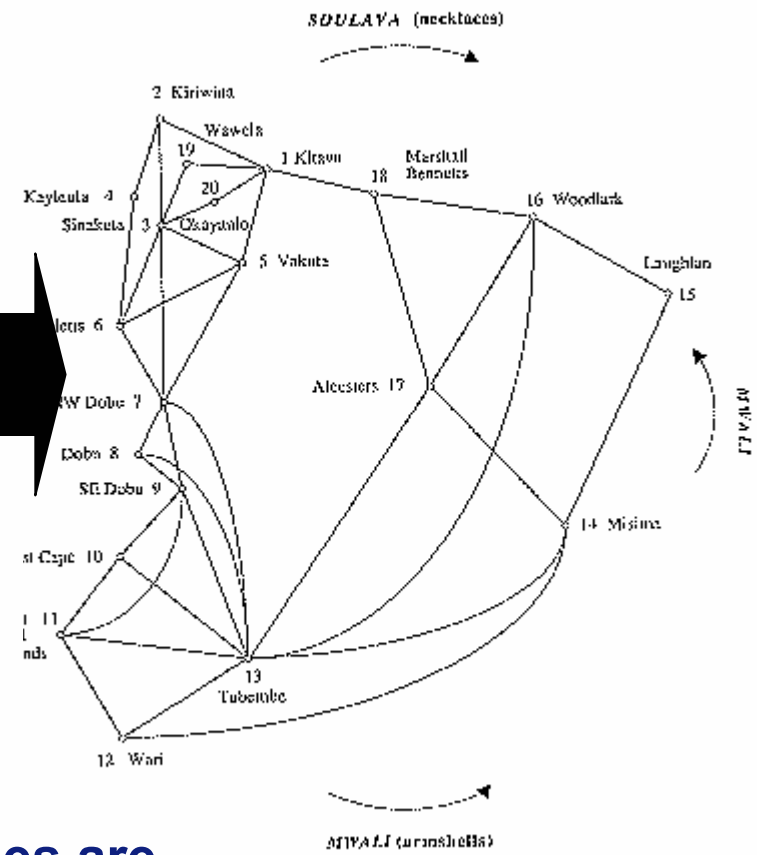
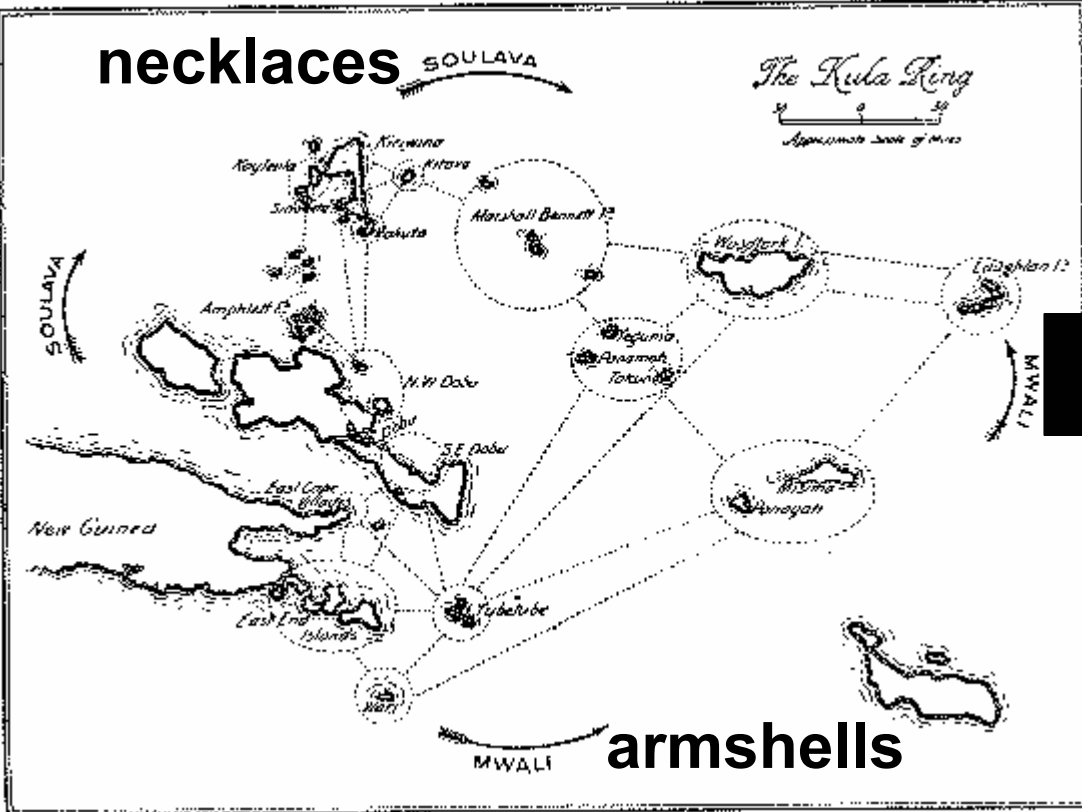


FIG. 5.1. The graph  $G$  of the kula ring

Hage and Harary formed a graph where edges are exchange relations and used random walkers to analyse the *global* properties of the system

Also Terrell 1977; Irwin 1983; Broodbank 2000

# Focus: Middle Bronze Age (MBA) Aegean

- Clear temporal delineation  
clear gaps (‘dark ages’) or shifts in record
  - c.2000BC distinct Minoan culture starts,  
and sail replaces oar
  - c.1500BC end of Minoan cultural dominance
- Physically largely self contained
  - questions regarding relationship to Egyptian culture



# Some Questions

- **The Knossos Question**

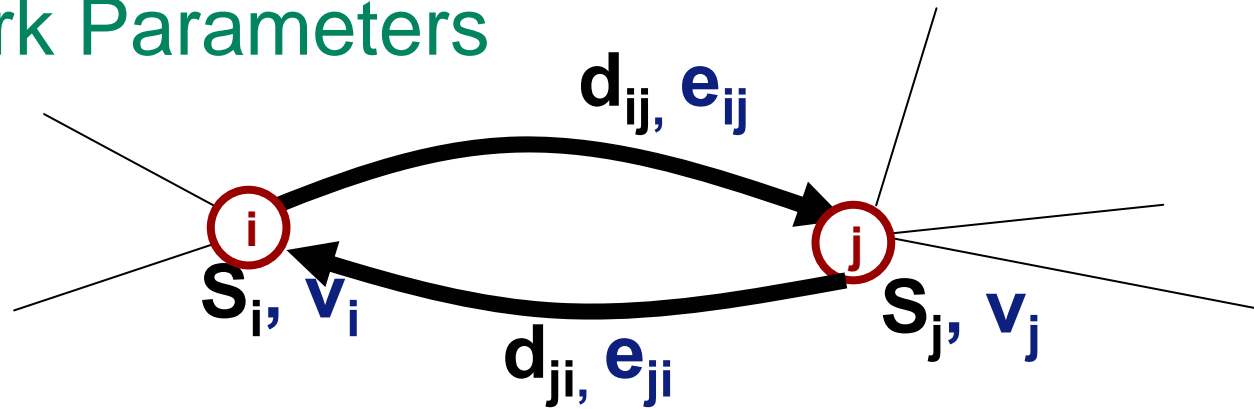
What is the connection between macro-scale development of regional networks and the emergence of a primary centre?

The palace at Knossos does not have the best local environment

- **Minoanisation**

What can explain the spread of and the variability in Minoan influence across the southern Aegean c.1700 BC?

# Network Parameters



- We want to find our optimal network given:-

## Inputs:

- Site sizes  $S_i$
- Site separation  $d_{ij}$

## Outputs:

- Site occupation  $v_i$
- Interaction levels  $e_{ij}$
- Total population  $\sum_j (S_i v_i)$
- Trade activity  $\sum_j (S_i v_i e_{ij})$

# Optimal Networks

- Adjust site and edge variables to optimise the 'cost'  $H$  of the network:

$$H = -\lambda E - \kappa L + jP + \mu T$$

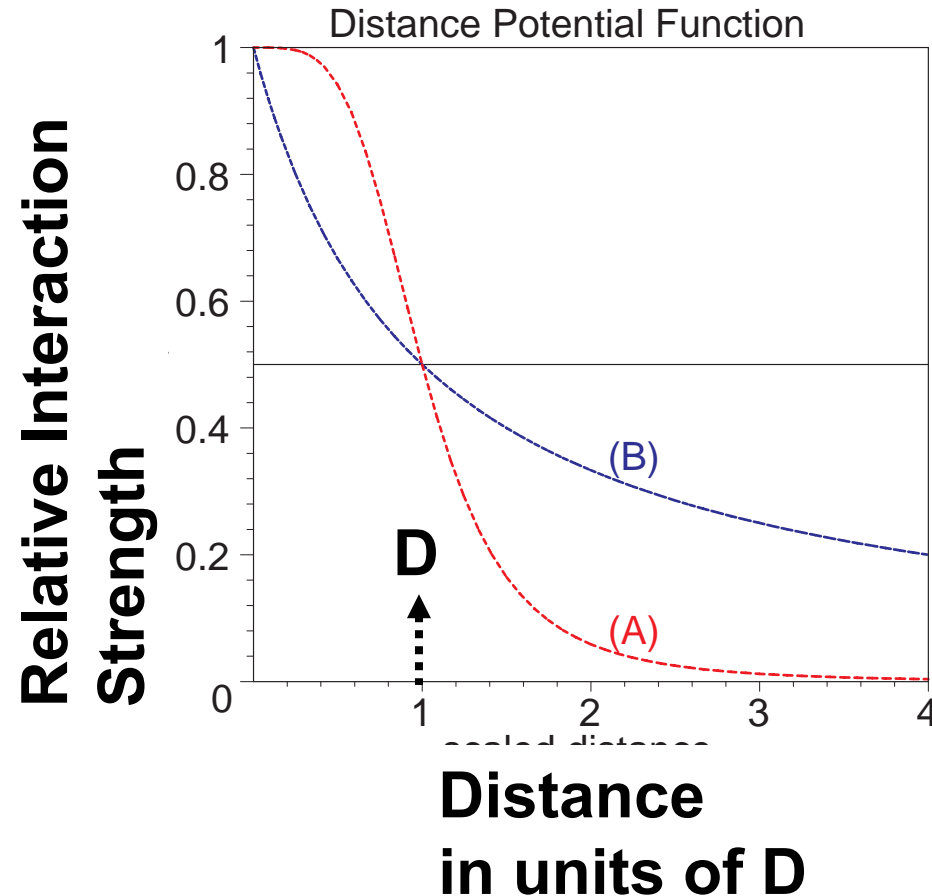
where

- **E – all exchange/trade**  
Increase parameter  $\lambda$  and interaction produces more benefits
- **L – all local production**  
Increase parameter  $\kappa$  and internal processes more profitable
- **P – total population**  
Increase parameter  $j$  and cost per person is increased
- **T – total strength of links**  
Increase parameter  $\mu$  and interaction links more expensive to maintain

# Distance Scale D

We use: **D=100km** for sail **D=10km** for rowing  
(after 2000BC) (pre 2000BC)

Interaction term for each pair of sites depends on distance  $d_{ij}$  between sites such that for distances longer than a scale  $D$  the benefit is zero i.e. no effective direct interaction



# Analysis

- Working with 34 sites
- Can not assign parameter values in model from physical data so make comparisons between different data sets

e.g. vary one parameter, hold rest fixed.

This represents slow evolution where system remains in effective equilibrium.

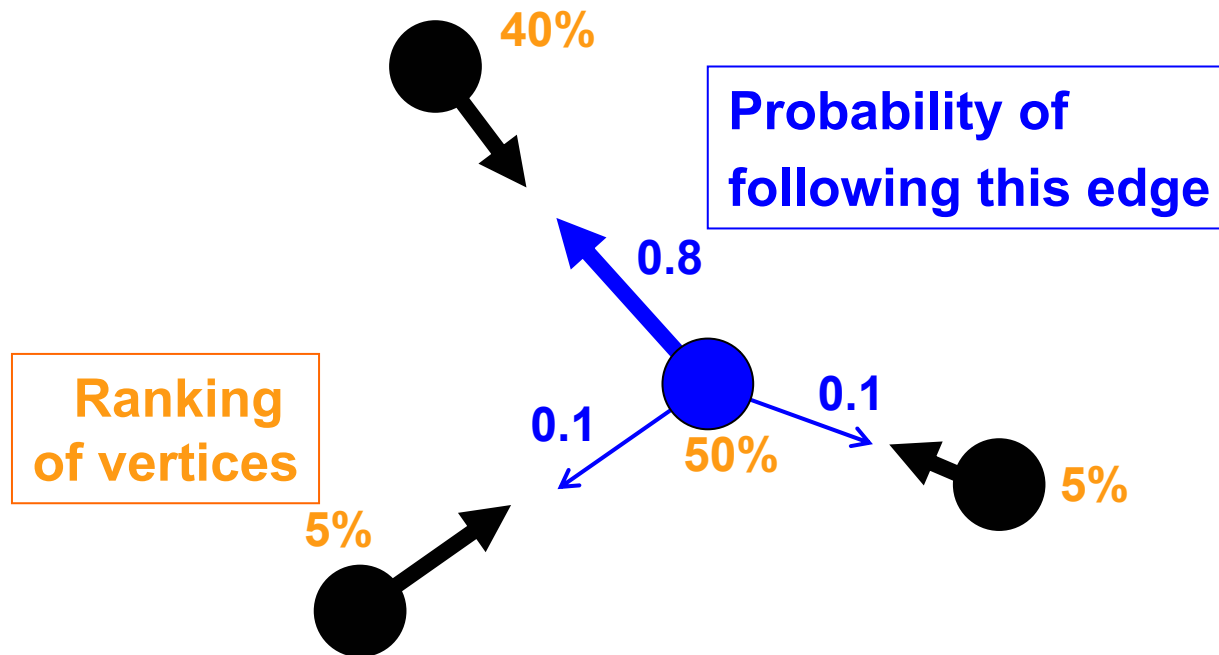
- For any given set of (reasonable) values:
  - a) can analyse intrinsic parameters
  - b) can perform further 'games' to analyse properties e.g. simulate trade in physical objects, cultural transmission models.



# Analysis Methods: Ranking

- The percentage of time spent at each node by an *imaginary* random walker on the network. The walker moves from site to site, choosing to follow a link with probability proportional to its strength. (Other choices possible).

⇒ **Measure of GLOBAL network properties**



As used by  
Hage &  
Harary 1991,  
and  
Google<sup>™</sup>  
UK

# The 34 Sites Used



# Analysis of Single Network

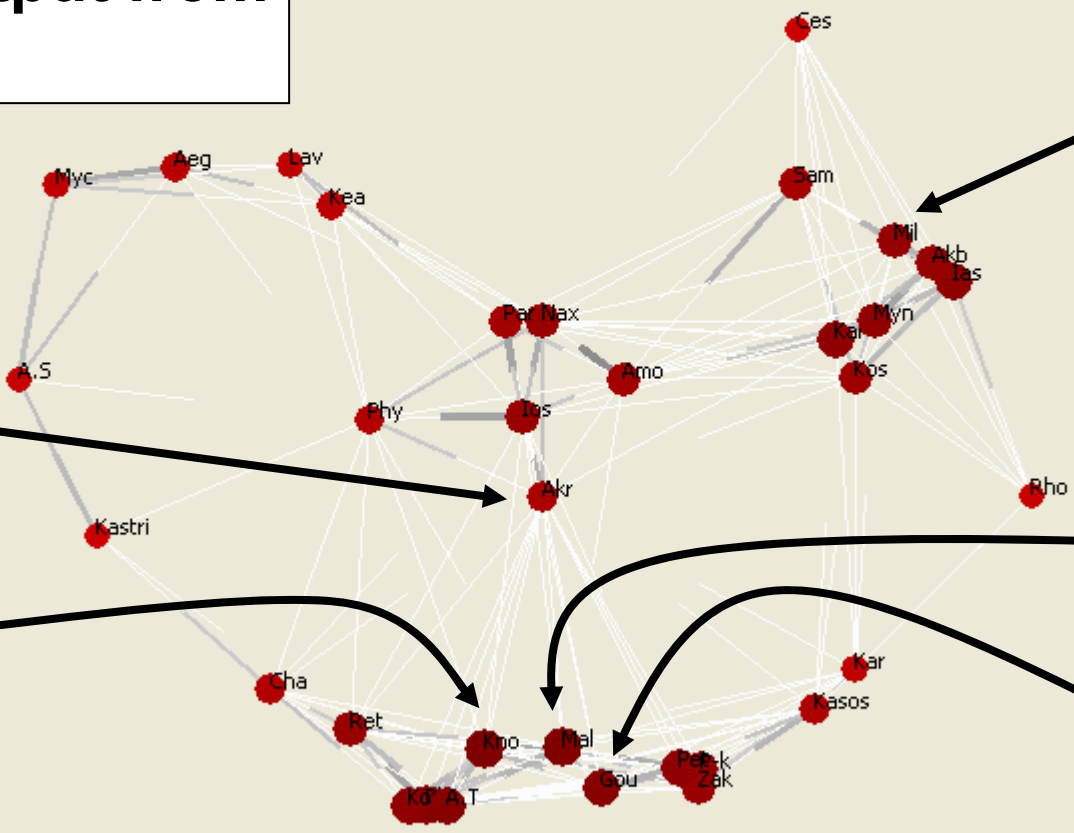
- The new few slides show the analysis of one result of our model
- Look for sites which are off any general trends

*$j=0, m=0.5, k=1.0, l=4.0$*

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0MCr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	

**Typical Output from  
*ariadne***



**Miletus**

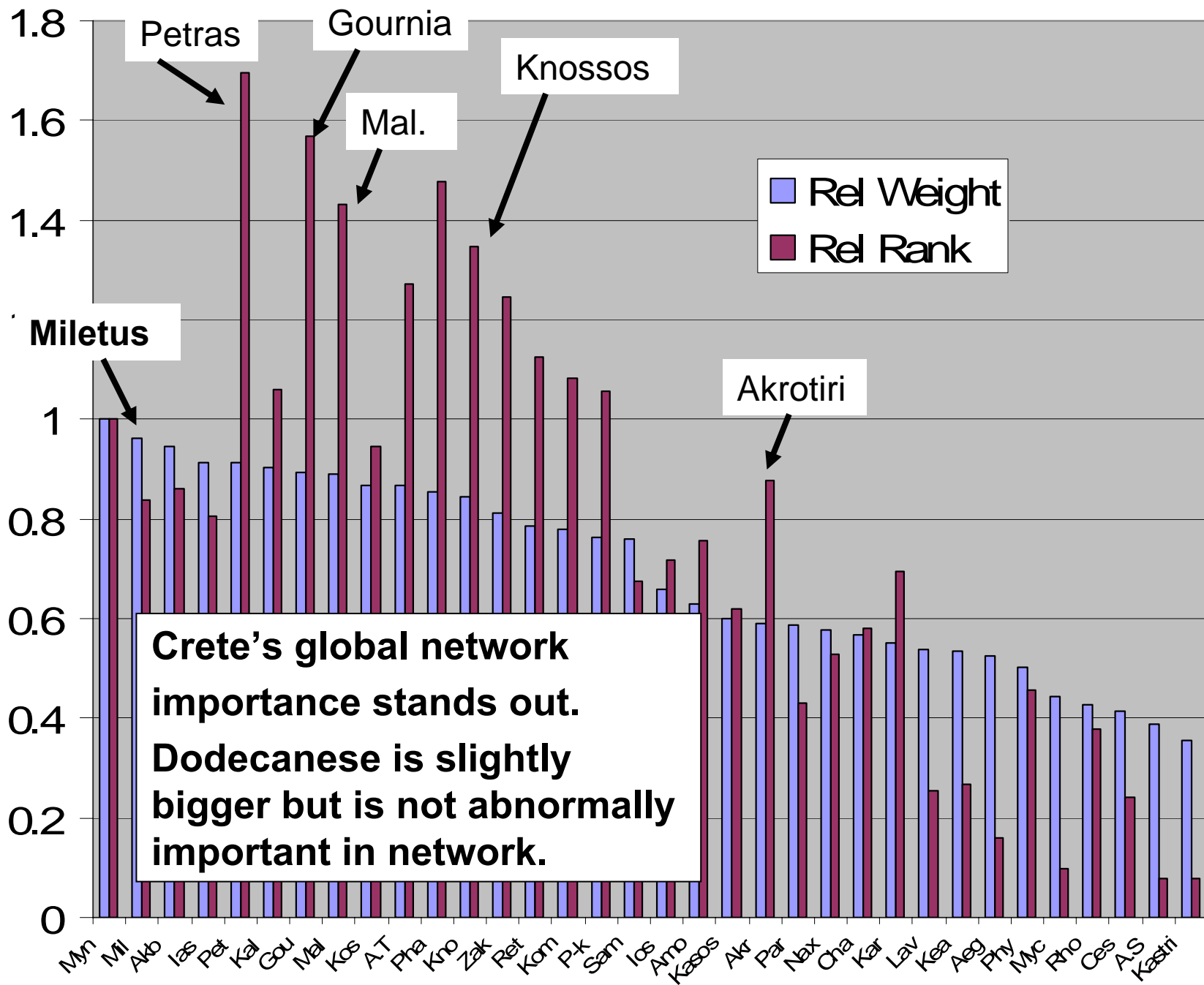
**Akrotiri**

**Malia**

**Knossos**

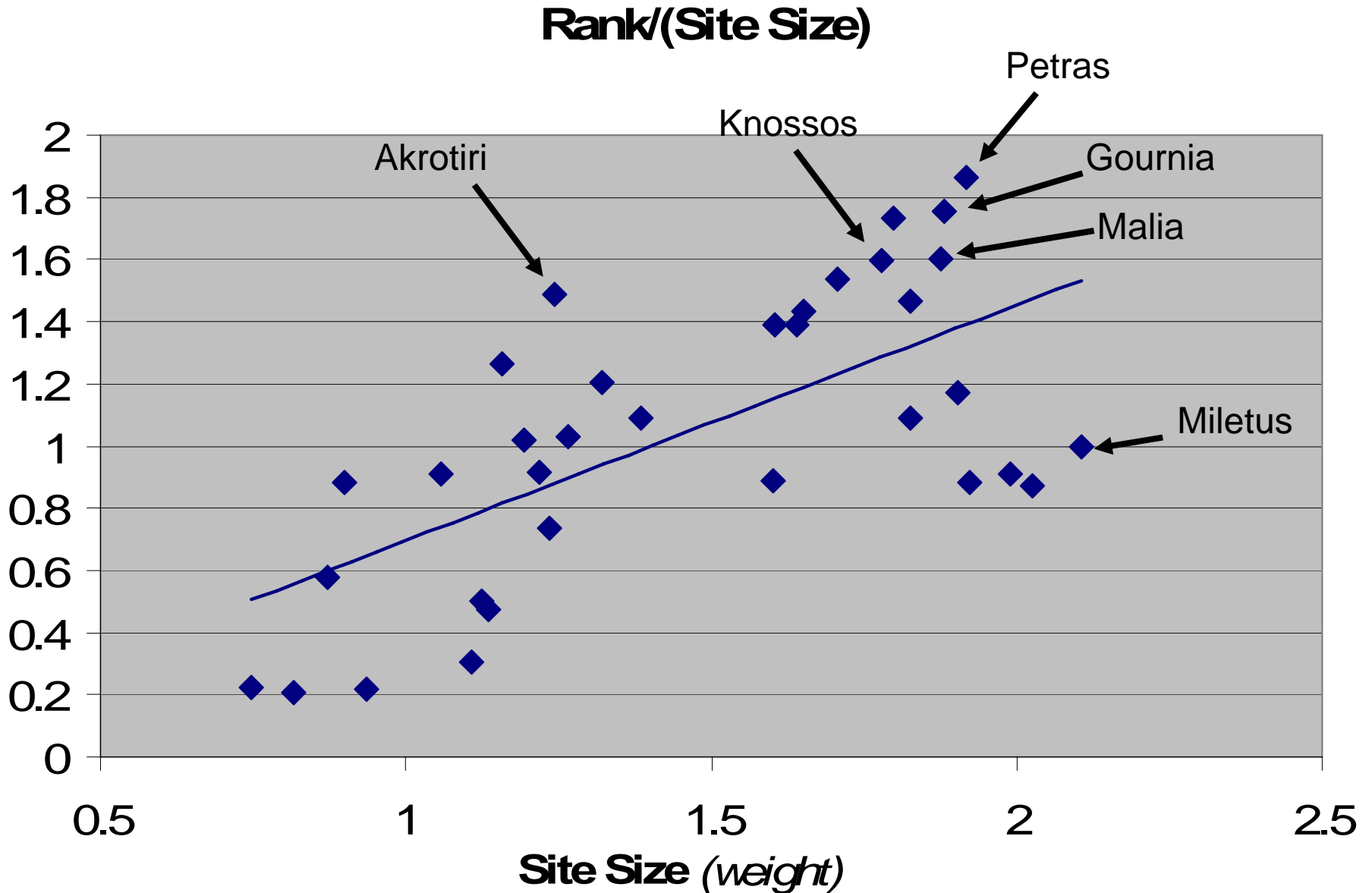
**Gournia**

Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.42	0.35	0.78	1.98
Site Out W.Strength	1.42	0.35	0.77	1.98
Edge Weight	0.04	0.08	0.0	0.45
Edge Value	0.03	0.06	0.0	0.34

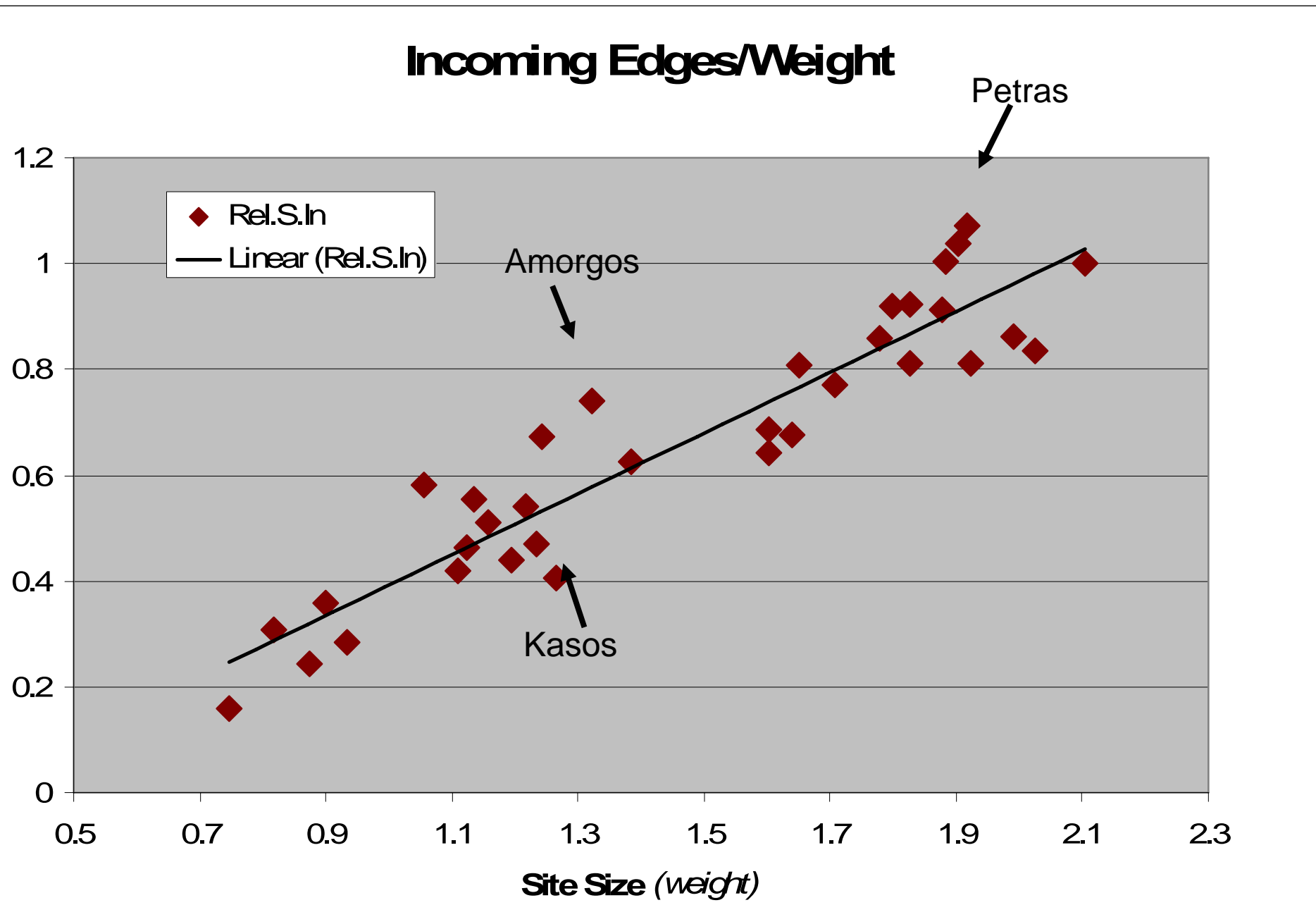




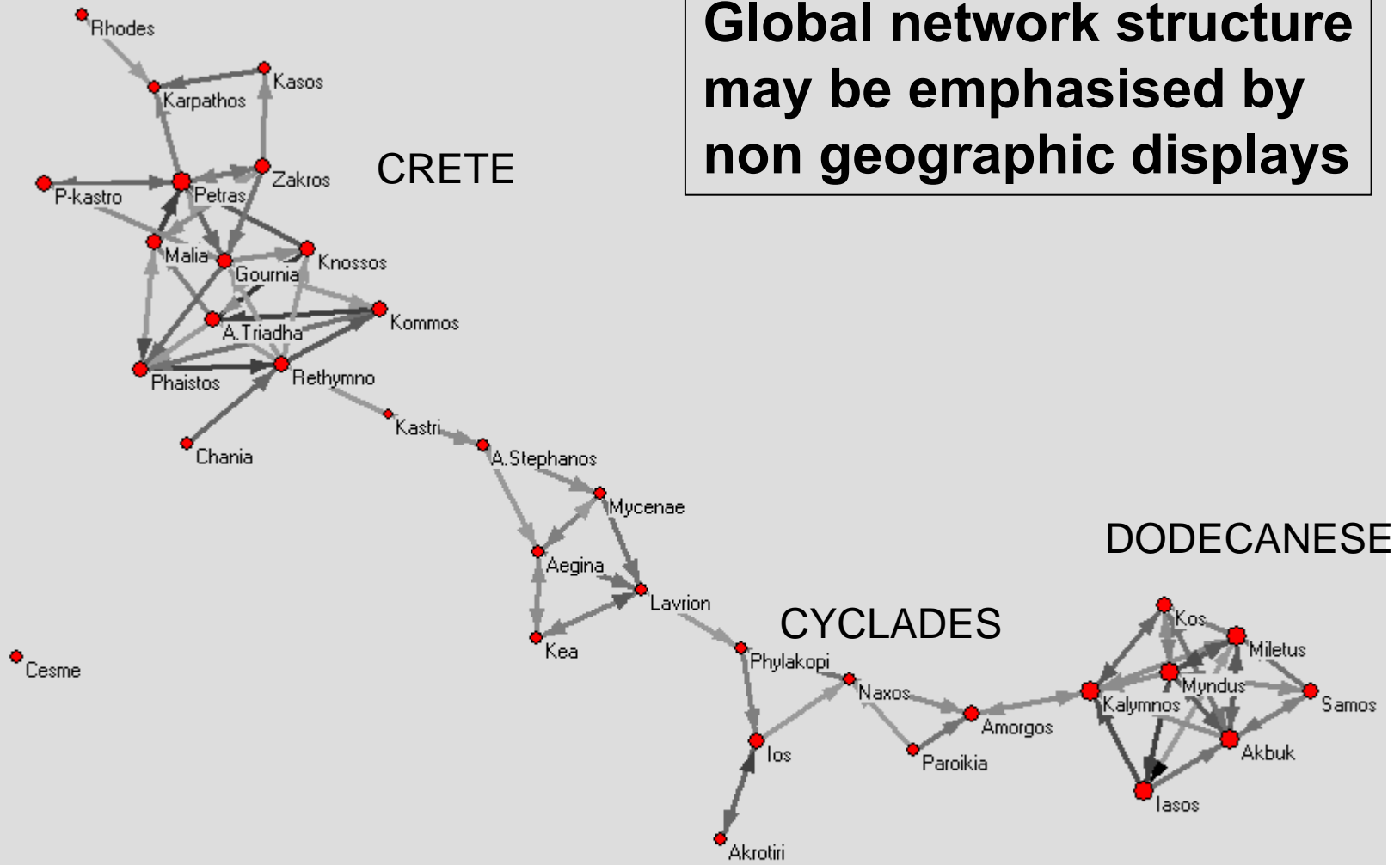
# Rank vs. Size shows Crete's is more important to the global network that its size suggests, not so for Dodecanese



# Local properties often scale closely with site size (weight)



**Global network structure  
may be emphasised by  
non geographic displays**



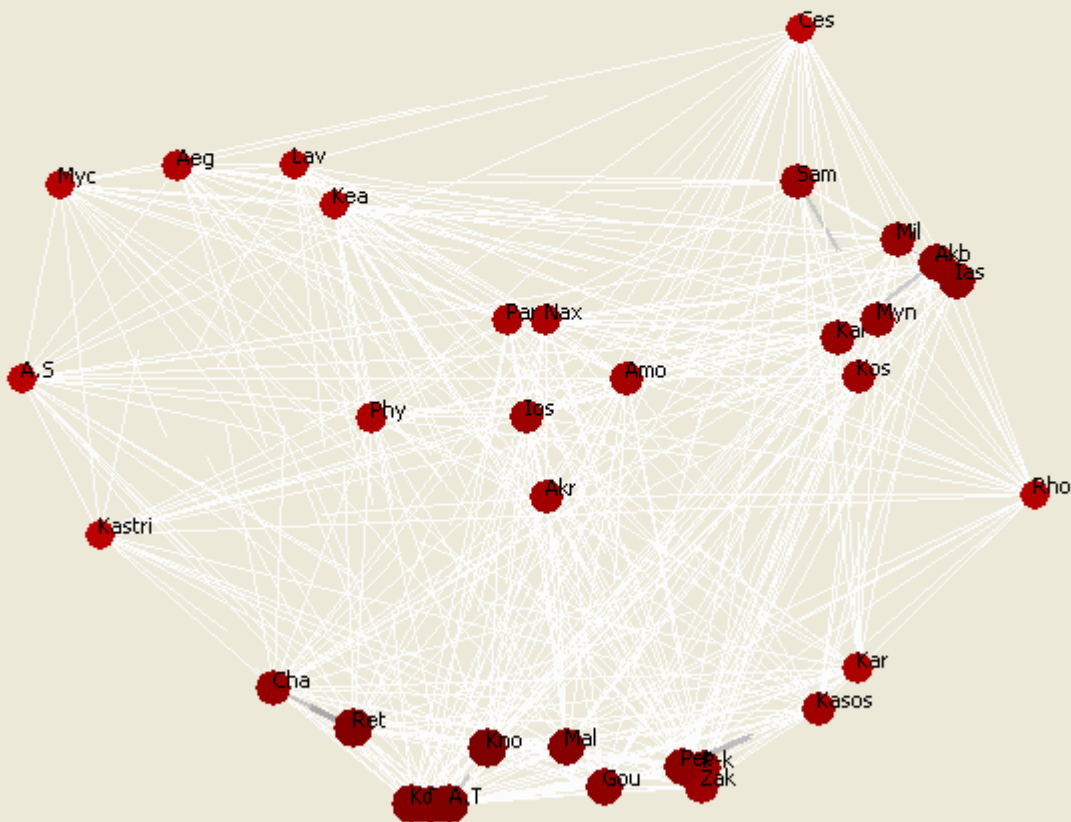
# Increasing Edge Cost ( $\mu$ )

## Next 7 slides

- for large interaction benefits ( $\lambda=4.0, j=0, \kappa=1.0$ )
- Increasing  $\mu$  causes edges to concentrate on decreasing profitable routes.
- The largest site size goes up while the smallest stays the same.
- Total cost in edges the same (as vertex out strength) but

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m-1.0j0.0k1.0b1.2s100.0MCR0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu -1.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 262144.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	

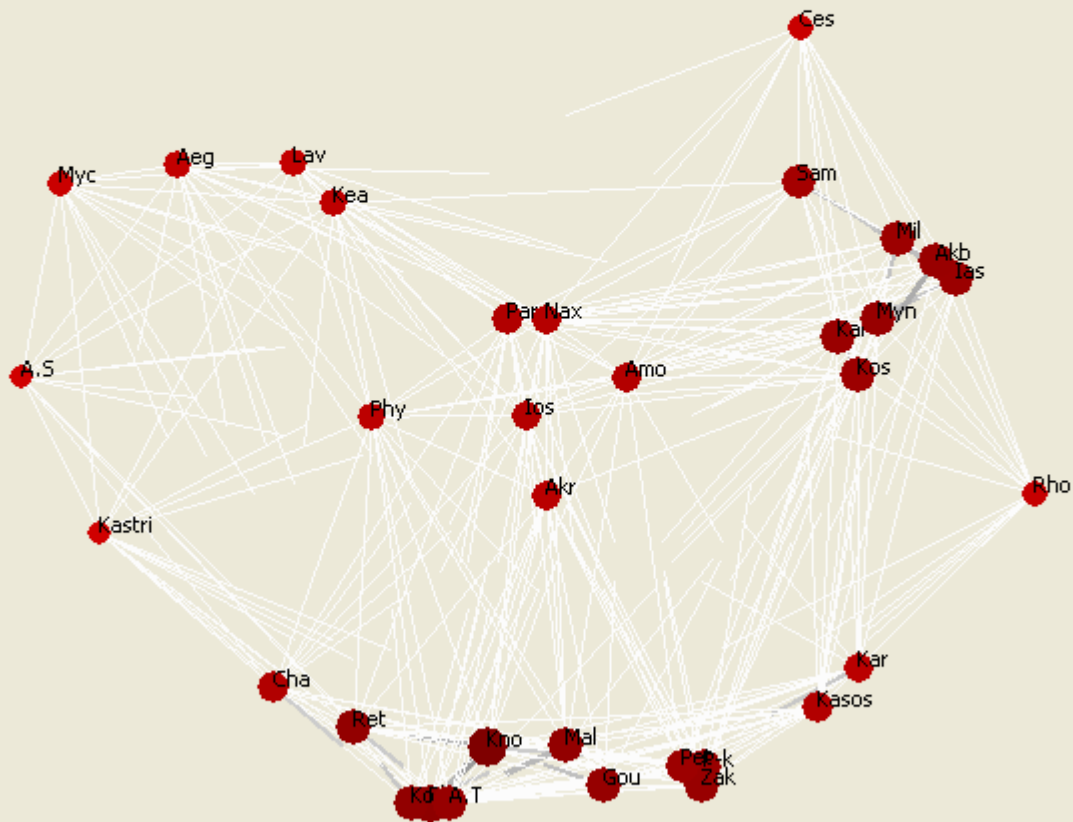


Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.07	0.2	0.74	1.4
Site Out W.Strength	1.07	0.2	0.74	1.4
Edge Weight	0.03	0.04	0.0	0.34
Edge Value	0.03	0.03	0.0	0.25



input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.0j0.0k1.0b1.2s100.0MCr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

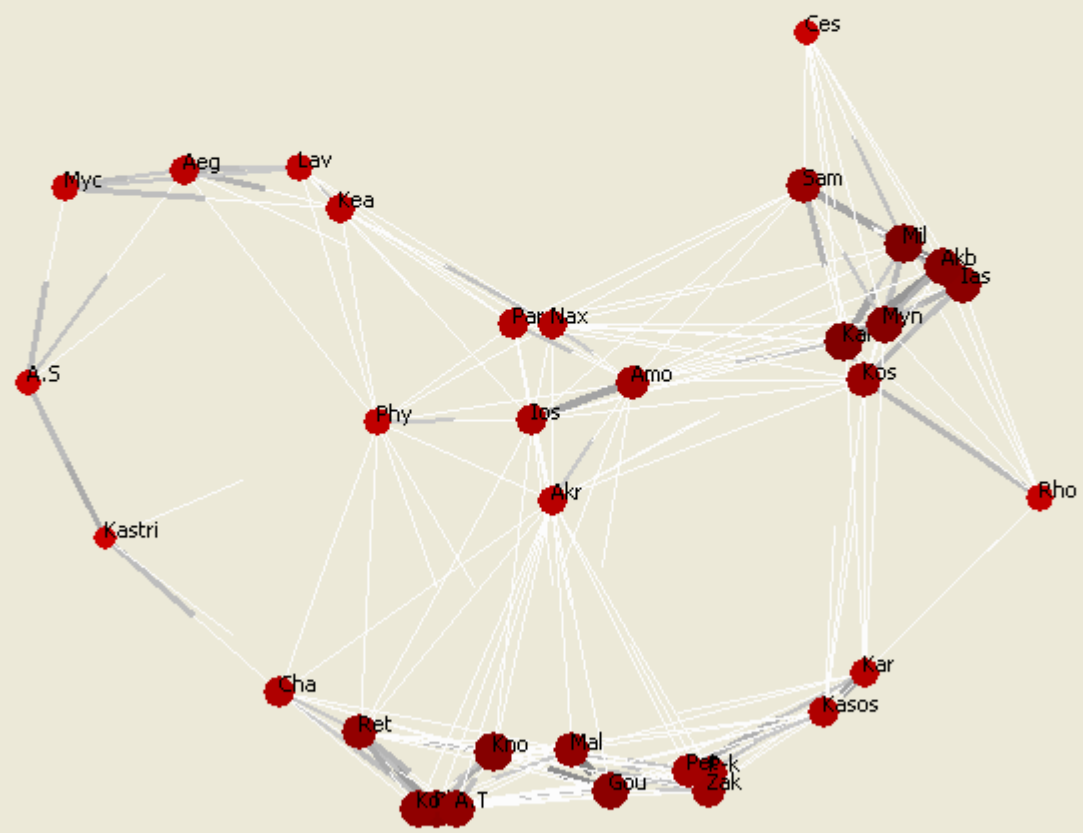
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.17	0.3	0.64	1.76
Site Out W.Strength	1.17	0.3	0.64	1.76
Edge Weight	0.03	0.05	0.0	0.39
Edge Value	0.03	0.04	0.0	0.23

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.43	0.37	0.79	2.03
Site Out W.Strength	1.43	0.37	0.79	2.03
Edge Weight	0.04	0.08	0.0	0.47
Edge Value	0.03	0.06	0.0	0.42

input file: aegean34

output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s100.0MCR0

Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1\_3

Monte Carlo Update

Limits on Out Strength 1.0

max vertex value 5.0

mu 1.0

j 0.0

kappa 1.0

lambda 4.0

b 1.2

distance scale 100.0

short distance scale 5.0

metric number 5.0

beta 524288.0

Zero Colour Frac 0.01

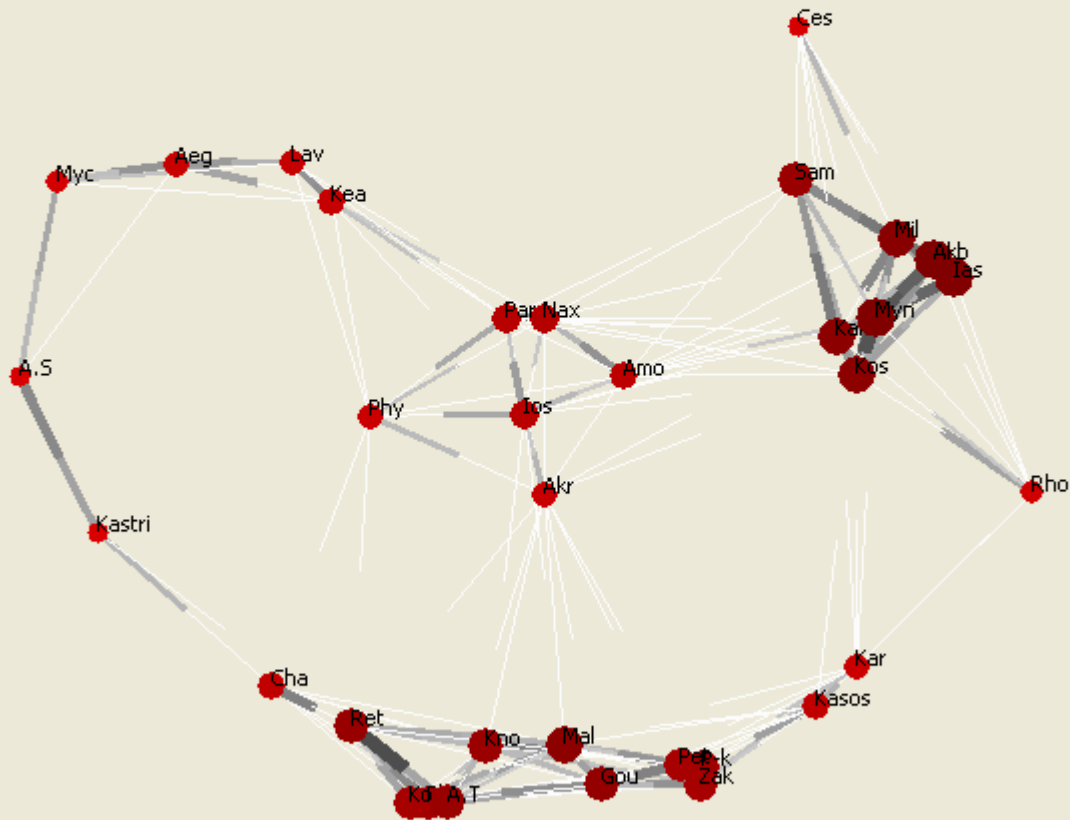
Min. Colour Frac 0.2

Relative Vertex Display

Absolute Edge Display, Max 1.0

Influence Range 1.0 (prob=0.5)

sites by Size



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.77	0.61	0.81	2.79
Site Out W.Strength	1.77	0.61	0.81	2.79
Edge Weight	0.05	0.12	0.0	0.7
Edge Value	0.03	0.07	0.0	0.53

input file: aegean34

output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s100.0Mcr0

Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1\_3

mu 1.0

b 1.2

beta 524288.0

Absolute Edge Display, Max 1.0

Monte Carlo Update

j 0.0

distance scale 100.0

Zero Colour Frac 0.01

Influence Range 1.0 (prob=0.5)

Limits on Out Strength 1.0

kappa 1.0

short distance scale 5.0

Min. Colour Frac 0.2

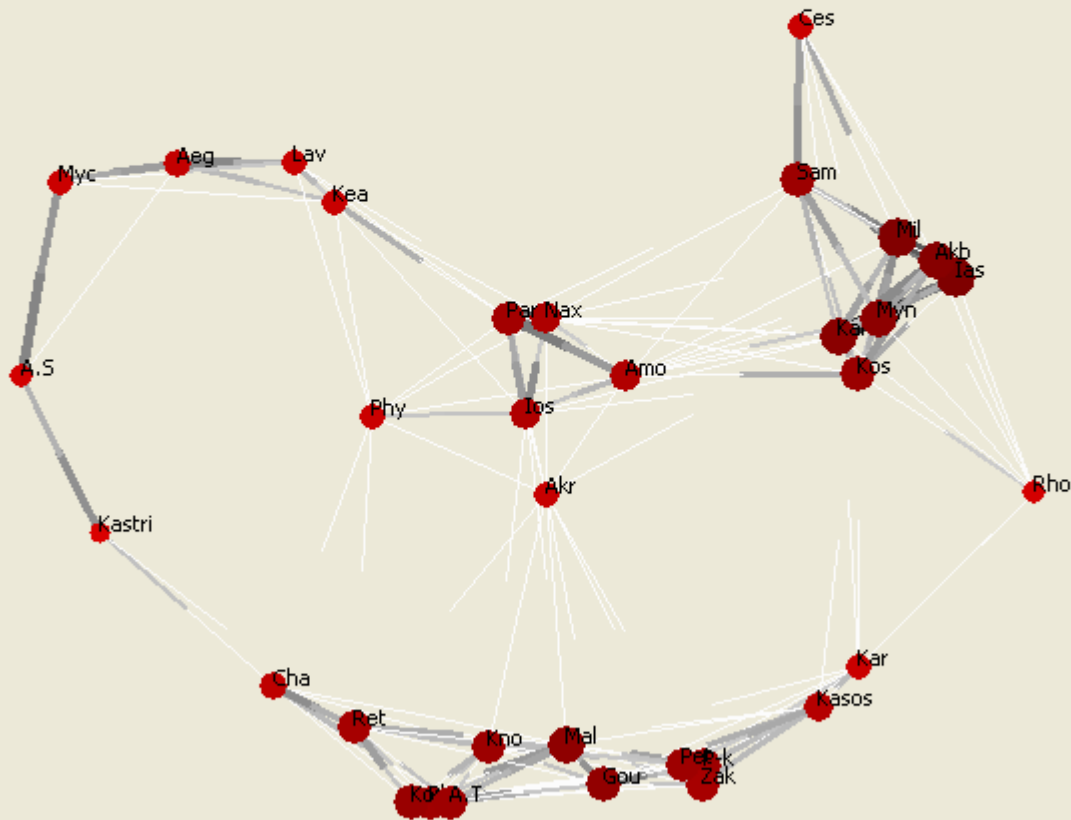
sites by Size

max vertex value 5.0

lambda 4.0

metric number 5.0

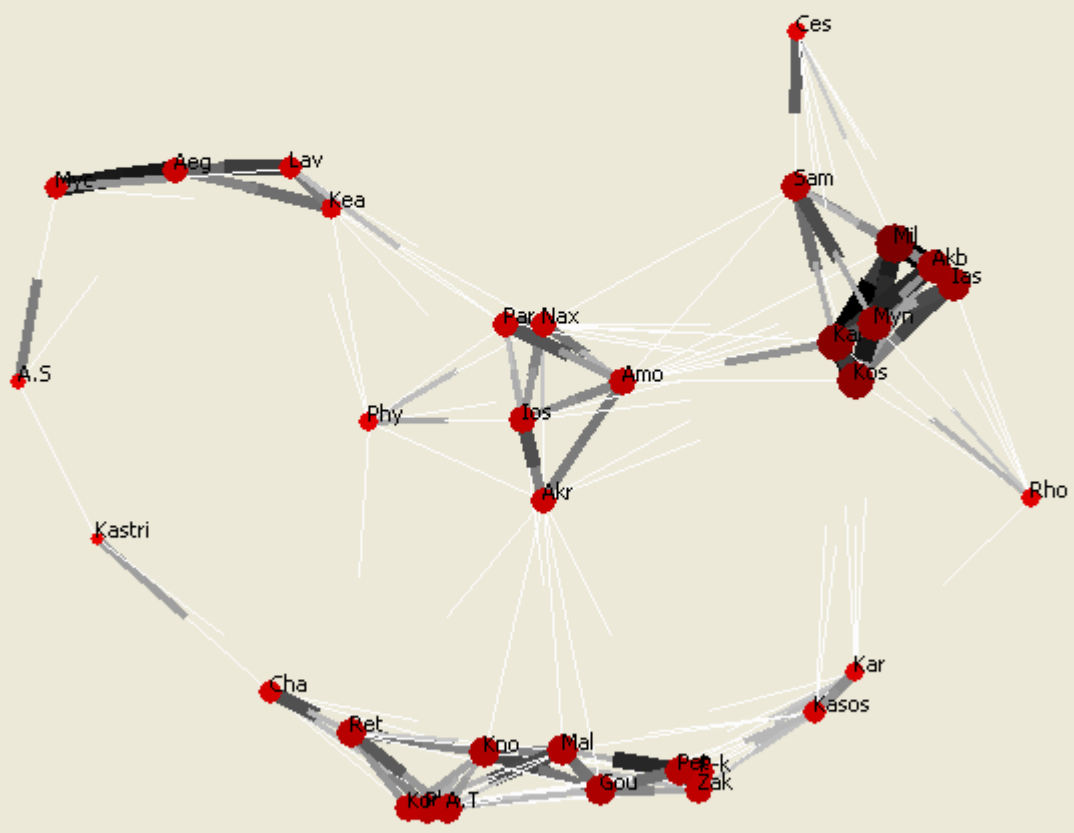
Relative Vertex Display



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.72	0.54	0.77	2.66
Site Out W.Strength	1.72	0.54	0.77	2.66
Edge Weight	0.05	0.11	0.0	0.81
Edge Value	0.03	0.07	0.0	0.56

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m1.5j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 1.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	

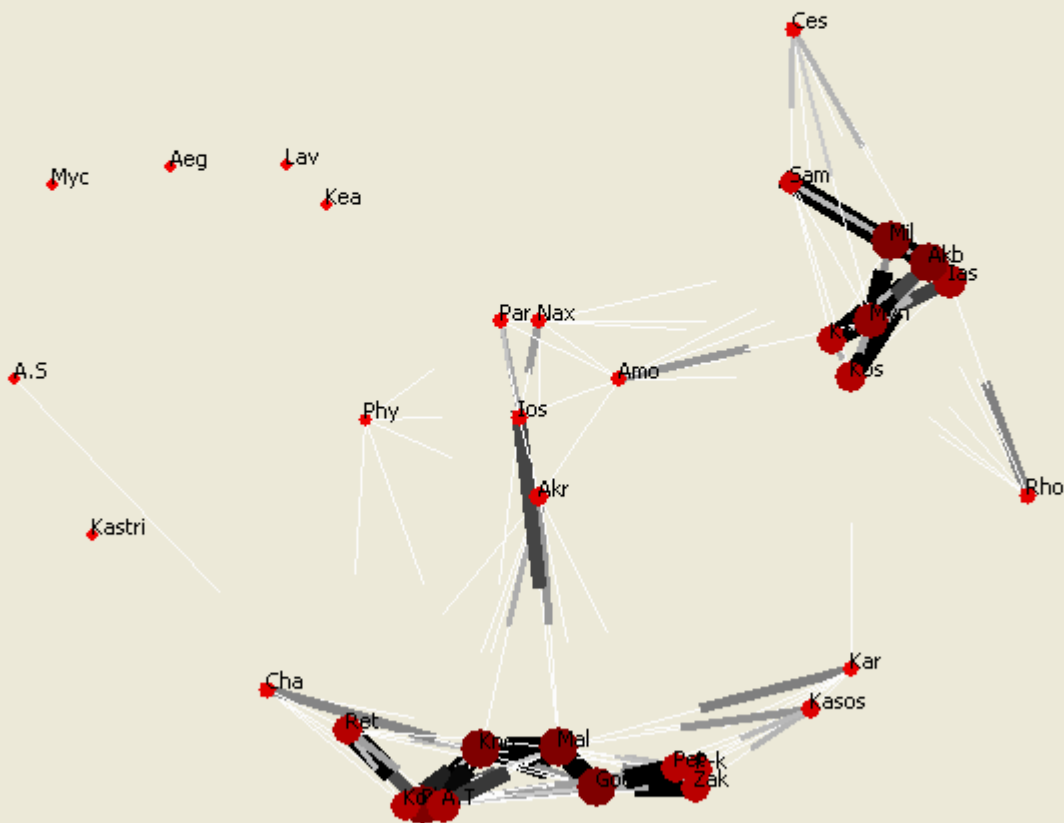


Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	2.32	0.99	0.64	4.62
Site Out W.Strength	2.32	0.99	0.64	4.62
Edge Weight	0.07	0.18	0.0	1.4
Edge Value	0.03	0.08	0.0	0.63



input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m2.0j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 2.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	2.24	1.66	0.46	5.0
Site Out W.Strength	2.17	1.74	0.06	5.0
Edge Weight	0.06	0.27	0.0	3.47
Edge Value	0.03	0.09	0.0	0.78

End of increasing  $\mu$  sequence

# Minoanisation Analysis Methods

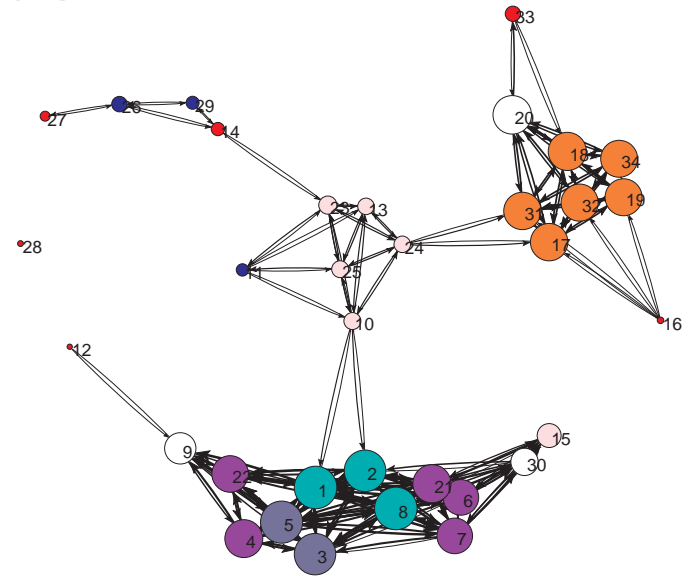
- **Diffusion**

Use random walkers doing variable short range walks to assess how ideas can percolate through system.

- **Cultural Transmission**

Use the networks produced here as substrate for well known models of cultural transmission (Bentley & Shennan 2003) and language transmission (Stauffer et al. 2006)

- based on copying (drift) and innovation (mutation) processes



# Summary

- Starting to extract basic results systematically
- Some behaviour looks interesting to an archaeologist
  - Crete and Dodecanese usually form strongest clusters
- Some types of behaviour do not appear to be possible
  - Greek mainland rarely gives significant sized sites
- Some factors seem to be playing a key role
  - small differences in physical distance from Crete may be significant
- **Many options remain to be explored**
  - improve distance data, more analysis tools, more what if scenarios, EBA vs MBA, general time evolution, other data sets

# Additional Material

More stuff ...

# PPA - Proximal Point Analysis

Most models focused on local interactions, often just nearest neighbour interactions

- Malta (*Renfrew & Level, 1979*)
- Geometric Greece (*Rihll & Wilson, 1991*)

- Proximal Point Analysis

Connect each vertex to 3 (or whatever) nearest neighbours

- (*Terrell 1977; Irwin 1983; Hage and Harary, 1991, 1996*)
- *EBA Aegean (Broodbank 2000)*
- *Vikings (Sindbæk, in prep.)*
- *Hypsistos Cult (Collar, in prep.)*

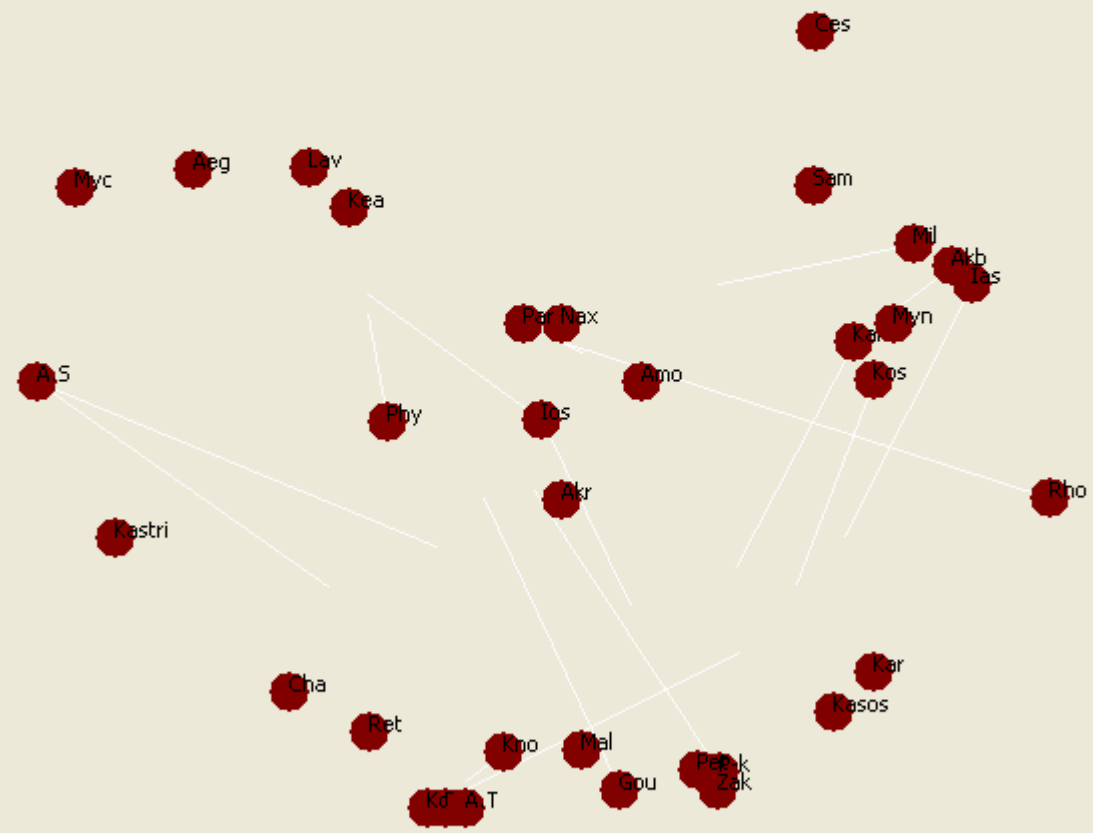


# Increasing Interaction Benefits ( $\lambda$ )

Next 5 slides ...

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 0.5
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	0.49	0.0	0.48	0.5
Site Out W.Strength	0.08	0.01	0.06	0.11
Edge Weight	0.0	0.0	0.0	0.02
Edge Value	0.0	0.0	0.0	0.03

input file: aegean34

output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr0

Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1\_3

mu 0.5

b 1.2

beta 524288.0

Absolute Edge Display, Max 1.0

Monte Carlo Update

j 0.0

distance scale 100.0

Zero Colour Frac 0.01

Influence Range 1.0 (prob=0.5)

Limits on Out Strength 1.0

kappa 1.0

short distance scale 5.0

Min. Colour Frac 0.2

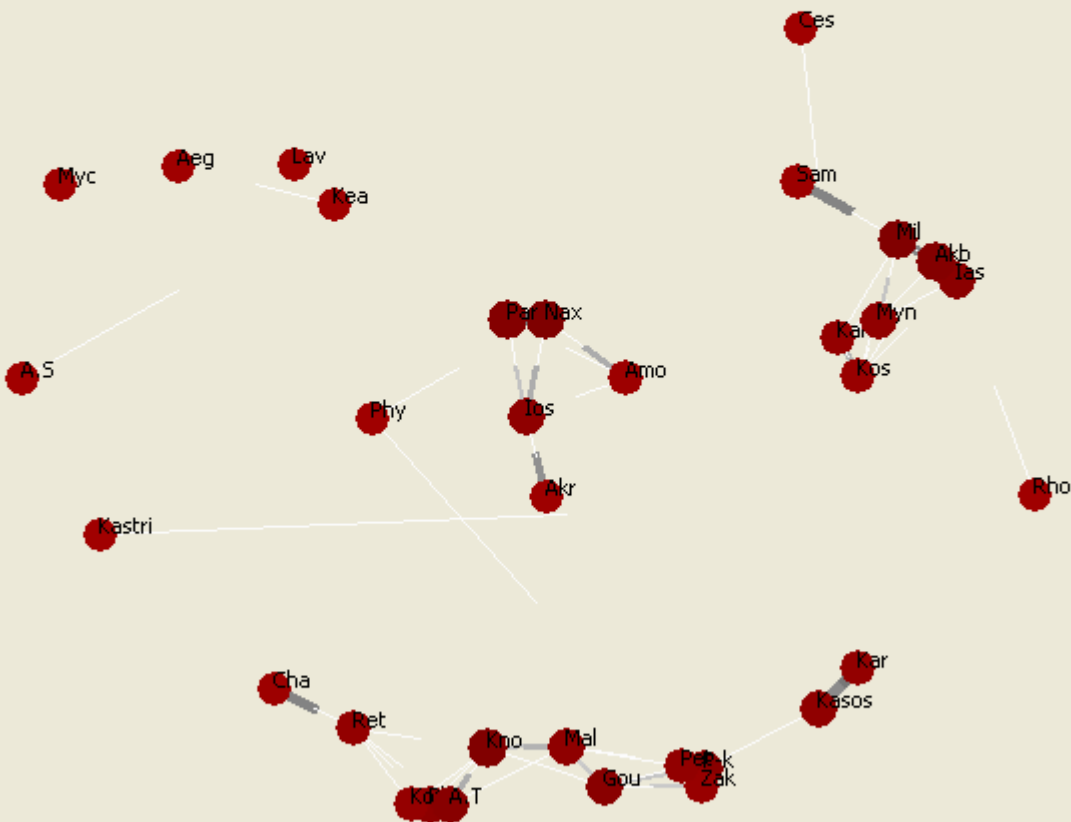
sites by Size

max vertex value 5.0

lambda 1.0

metric number 5.0

Relative Vertex Display



Quantity/Value

Site Weight

Site Out W.Strength

Edge Weight

Edge Value

Average

0.56

0.44

0.01

0.02

Sigma

0.06

0.22

0.06

0.1

Minimum

0.49

0.06

0.0

0.0

Maximum

0.66

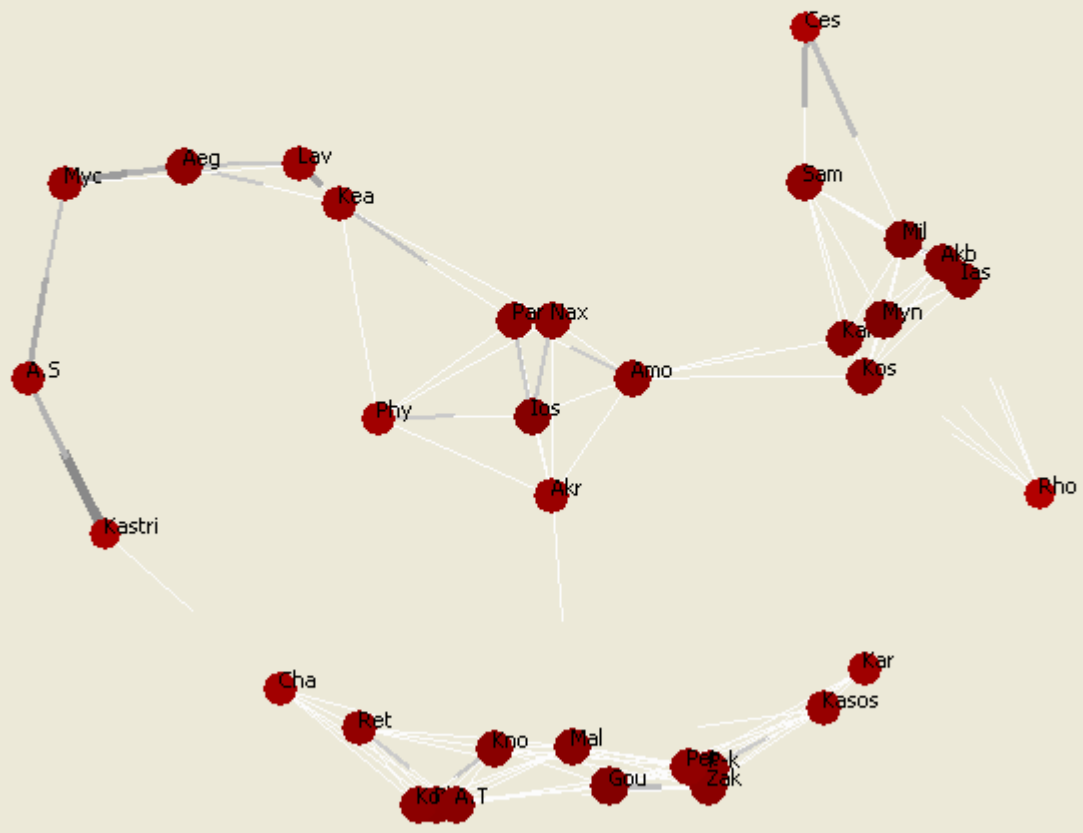
0.66

0.64

0.96

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0MCr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

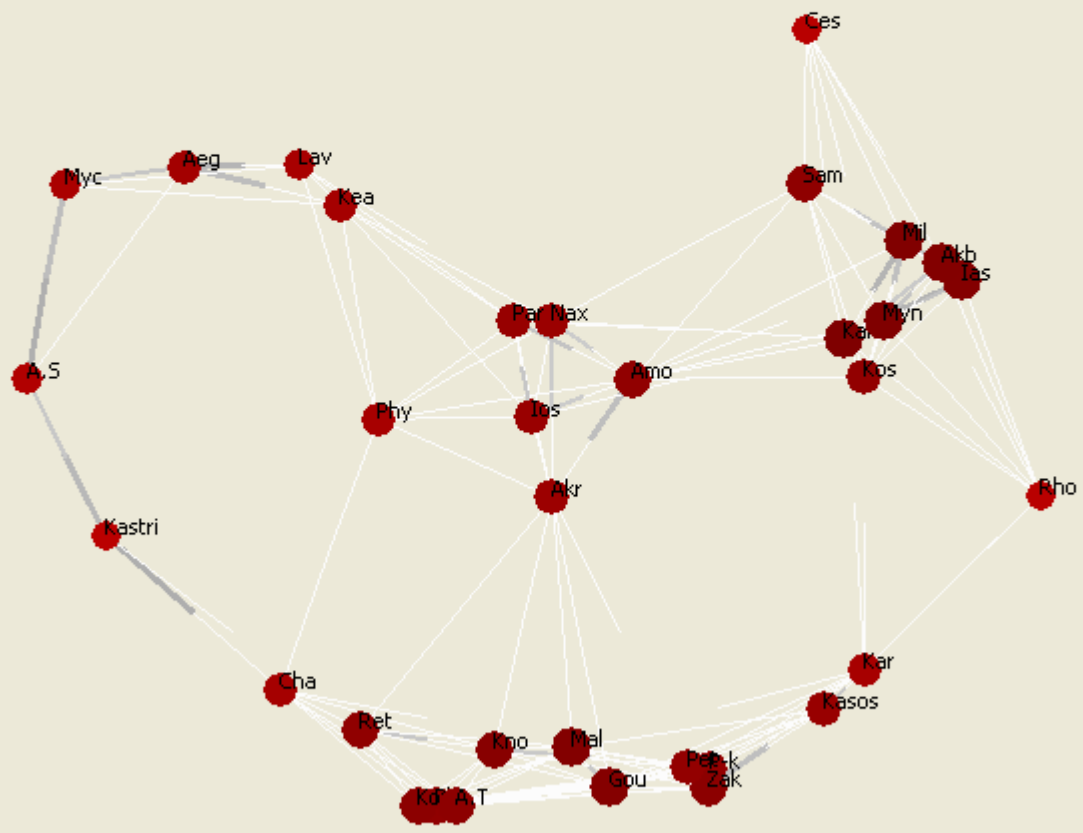
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 2.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	0.74	0.08	0.53	0.87
Site Out W.Strength	0.74	0.09	0.52	0.87
Edge Weight	0.02	0.06	0.0	0.46
Edge Value	0.03	0.08	0.0	0.79

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0MCr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

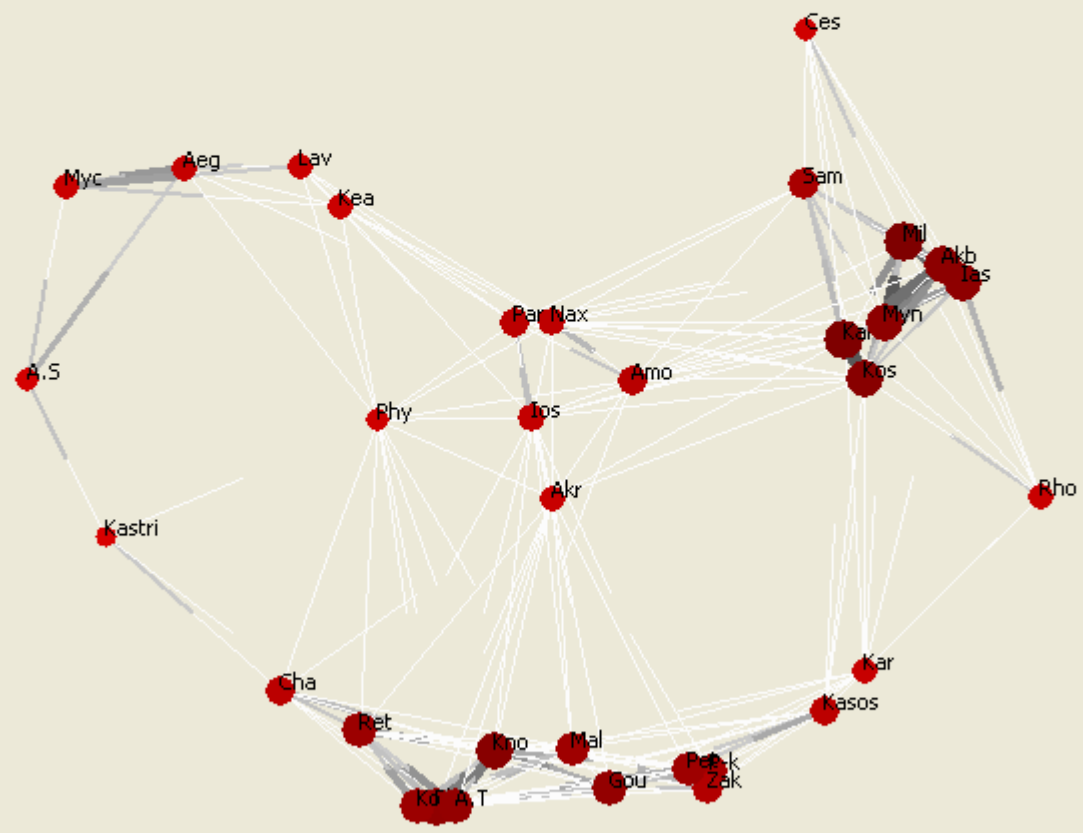
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 3.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	0.97	0.16	0.65	1.2
Site Out W.Strength	0.97	0.16	0.65	1.2
Edge Weight	0.03	0.06	0.0	0.32
Edge Value	0.03	0.06	0.0	0.49

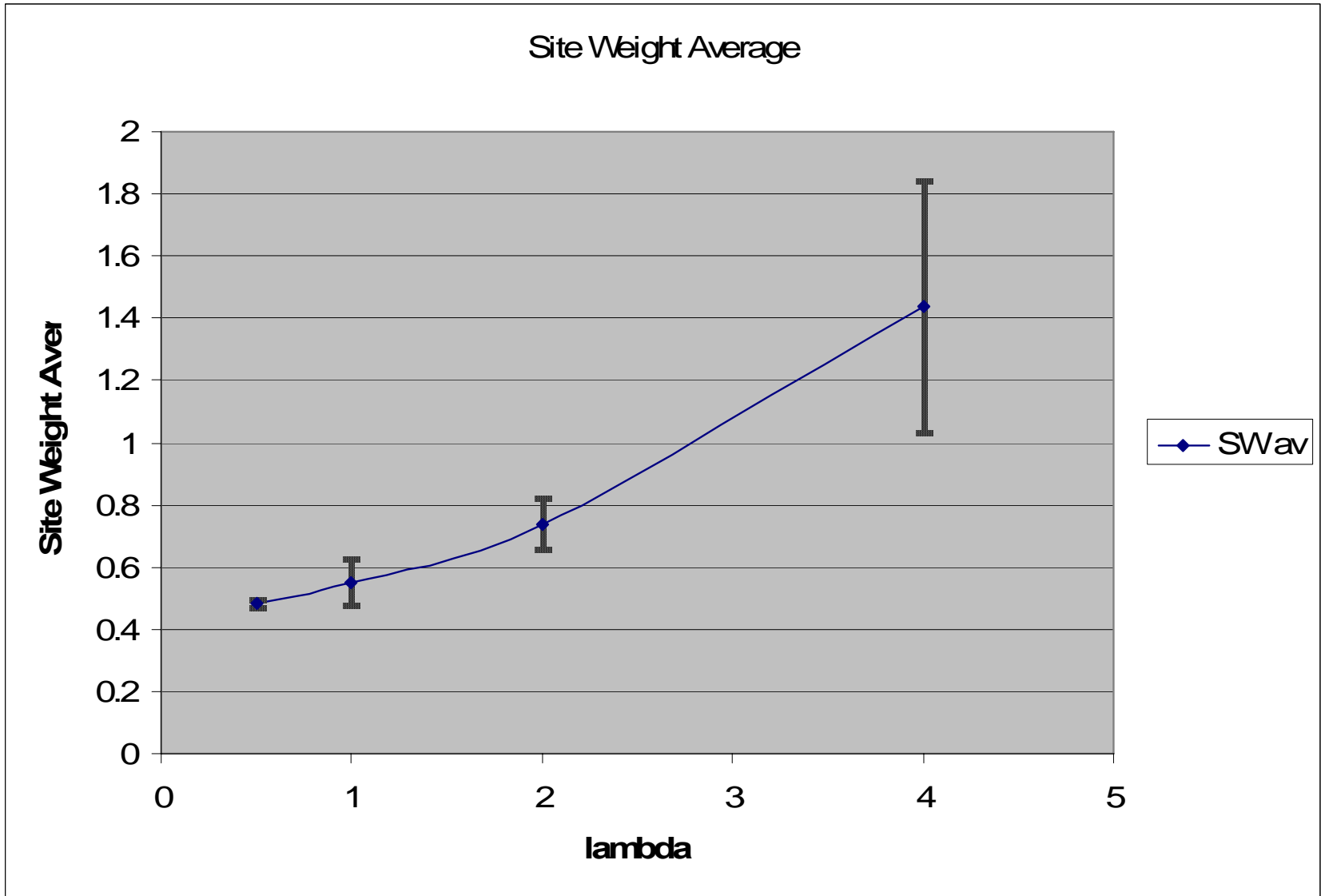
input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.52	0.51	0.73	2.39
Site Out w.Strength	1.51	0.51	0.73	2.39
Edge Weight	0.04	0.09	0.0	0.65
Edge Value	0.03	0.06	0.0	0.38

# End of increasing $\lambda$ sequence



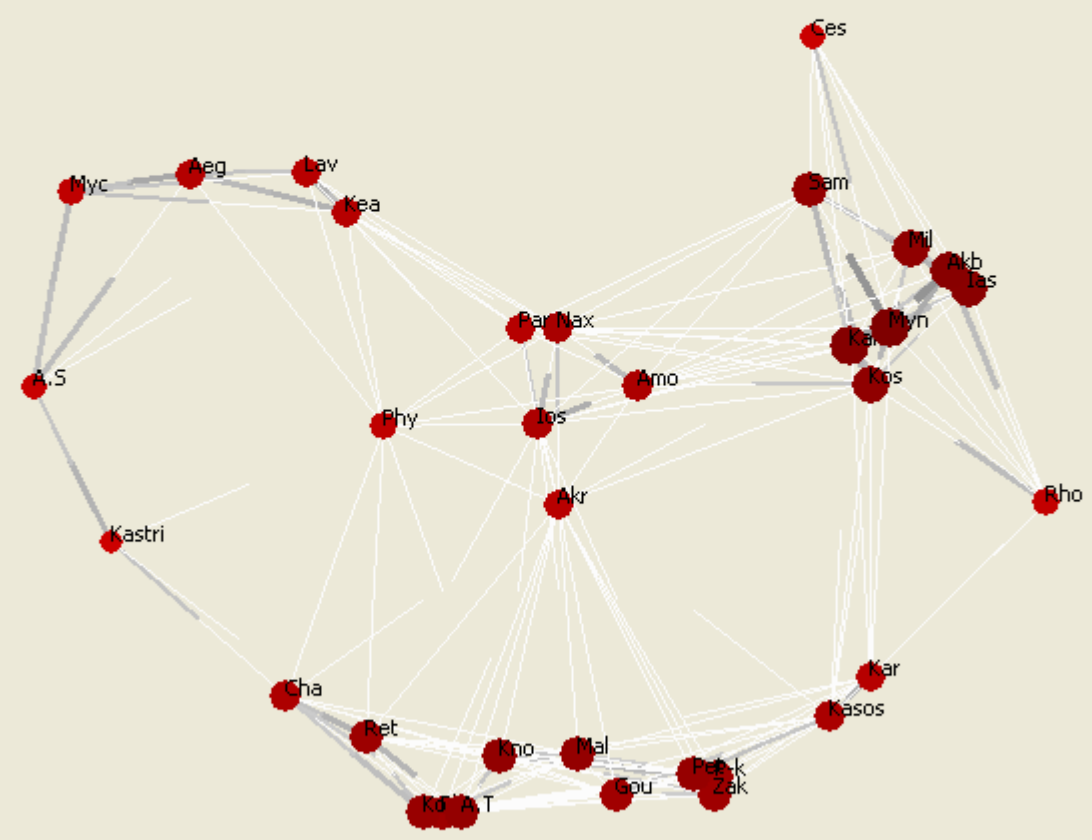


# Statistical Variation Constant Values

- The variables are held constant so simple statistical variations are evident
- These are reasonable, strengths of individual components vary by reasonable amounts, the details remain similar.

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0MCR0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

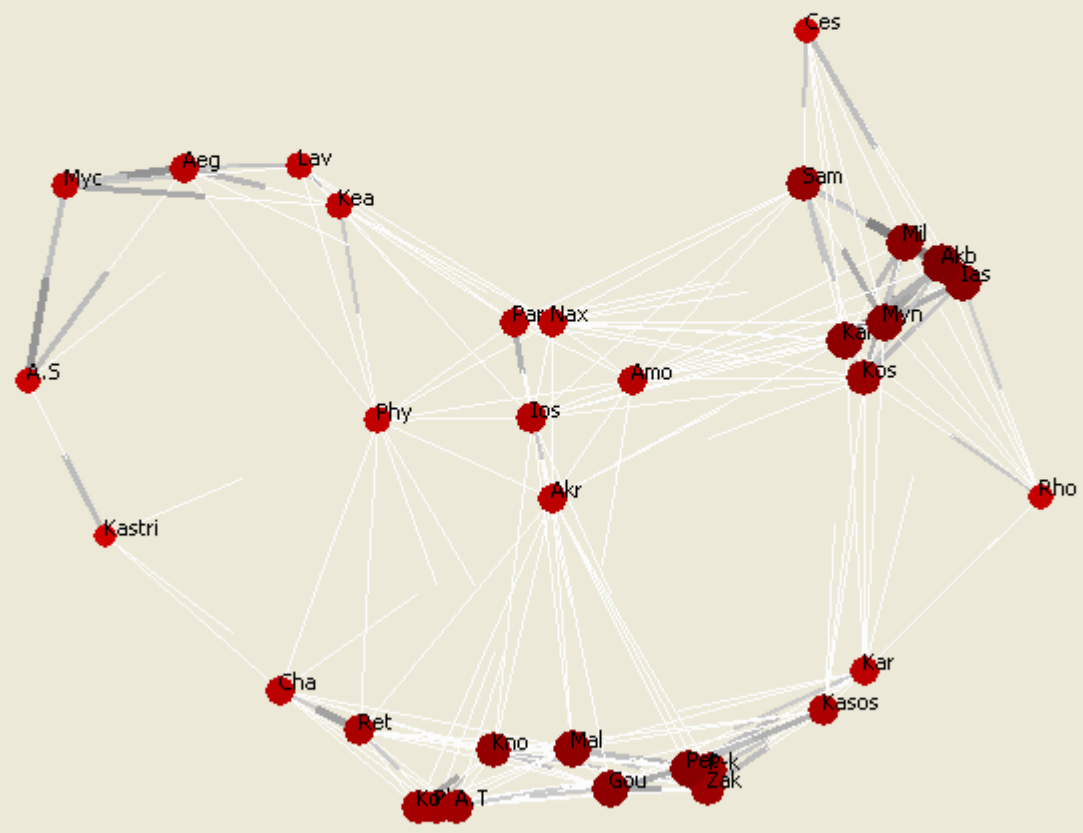
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.38	0.33	0.77	1.99
Site Out W.Strength	1.38	0.33	0.77	1.99
Edge Weight	0.04	0.08	0.0	0.42
Edge Value	0.03	0.06	0.0	0.38

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr1  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

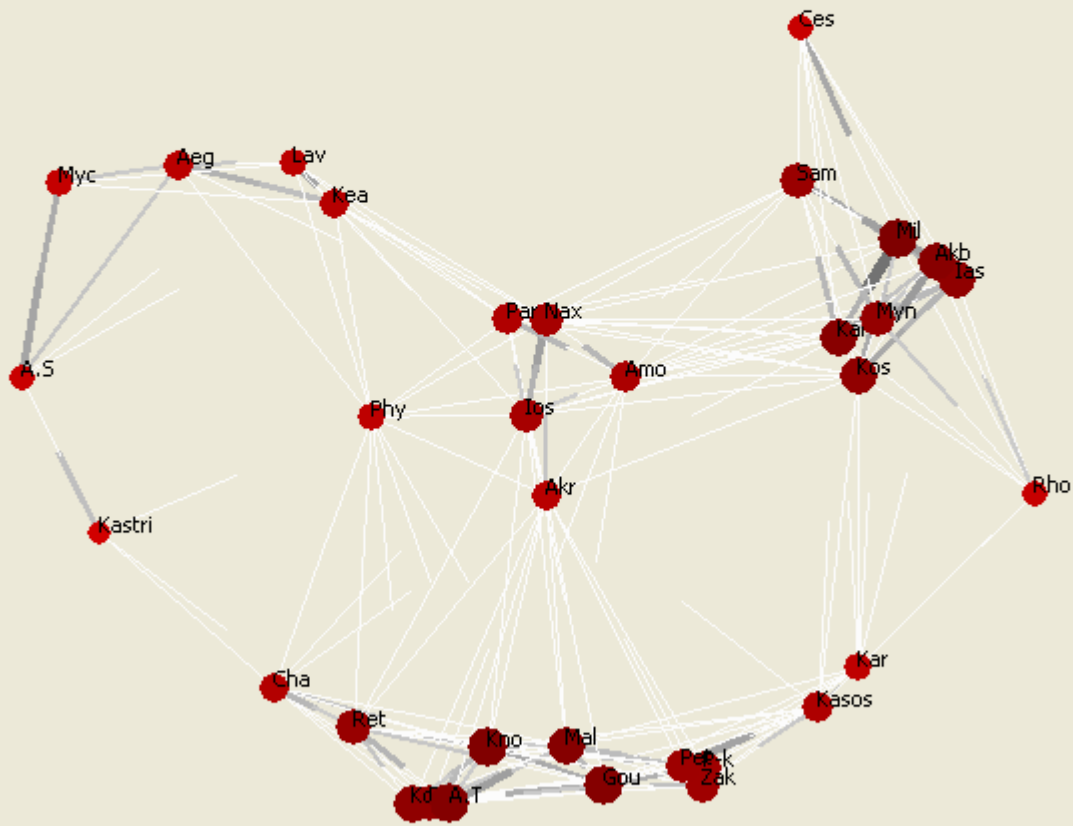
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.42	0.38	0.72	2.12
Site Out W.Strength	1.42	0.38	0.72	2.12
Edge Weight	0.04	0.08	0.0	0.49
Edge Value	0.03	0.06	0.0	0.48

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr2  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.45	0.39	0.72	2.05
Site Out W.Strength	1.45	0.39	0.72	2.05
Edge Weight	0.04	0.08	0.0	0.55
Edge Value	0.03	0.06	0.0	0.4

input file: aegean34

output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr3

Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1\_3

mu 0.5

b 1.2

beta 524288.0

Absolute Edge Display, Max 1.0

Monte Carlo Update

j 0.0

distance scale 100.0

Zero Colour Frac 0.01

Influence Range 1.0 (prob=0.5)

Limits on Out Strength 1.0

kappa 1.0

short distance scale 5.0

Min. Colour Frac 0.2

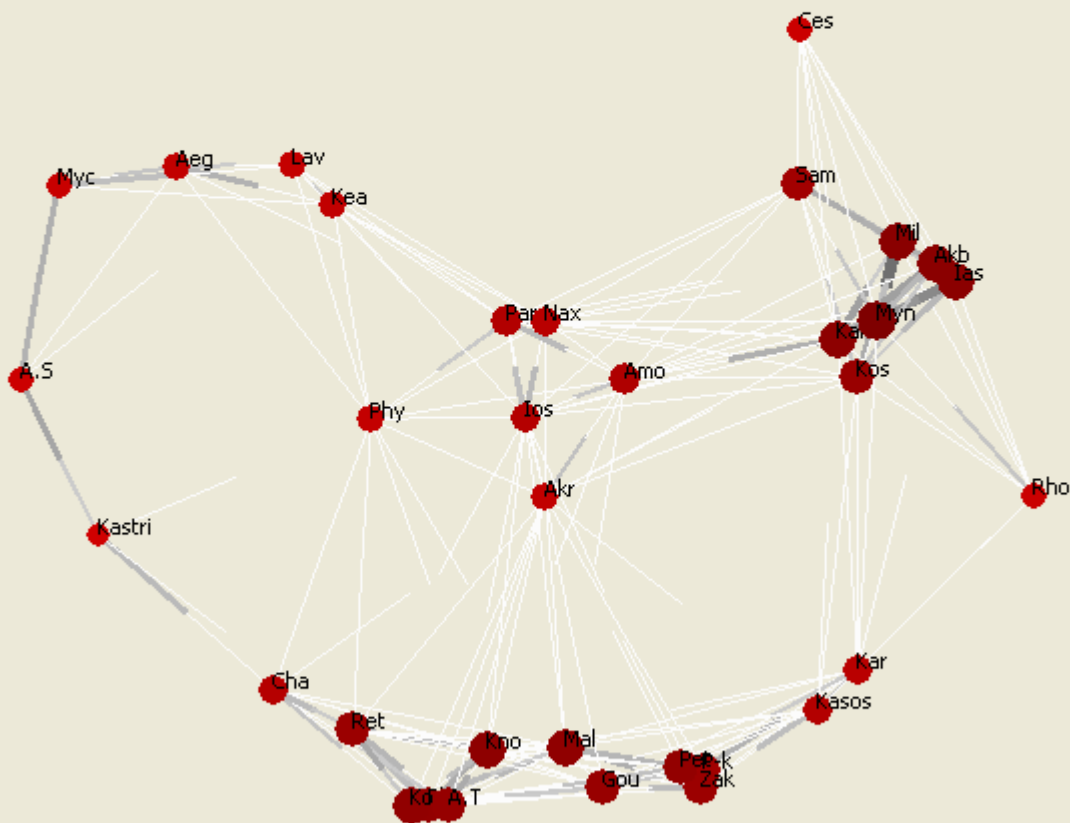
sites by Size

max vertex value 5.0

lambda 4.0

metric number 5.0

Relative Vertex Display



Quantity/Value

Site Weight

Site Out W.Strength

Edge Weight

Edge Value

Average

1.44

1.44

0.04

0.03

Sigma

0.4

0.41

0.08

0.06

Minimum

0.79

0.79

0.0

0.0

Maximum

2.15

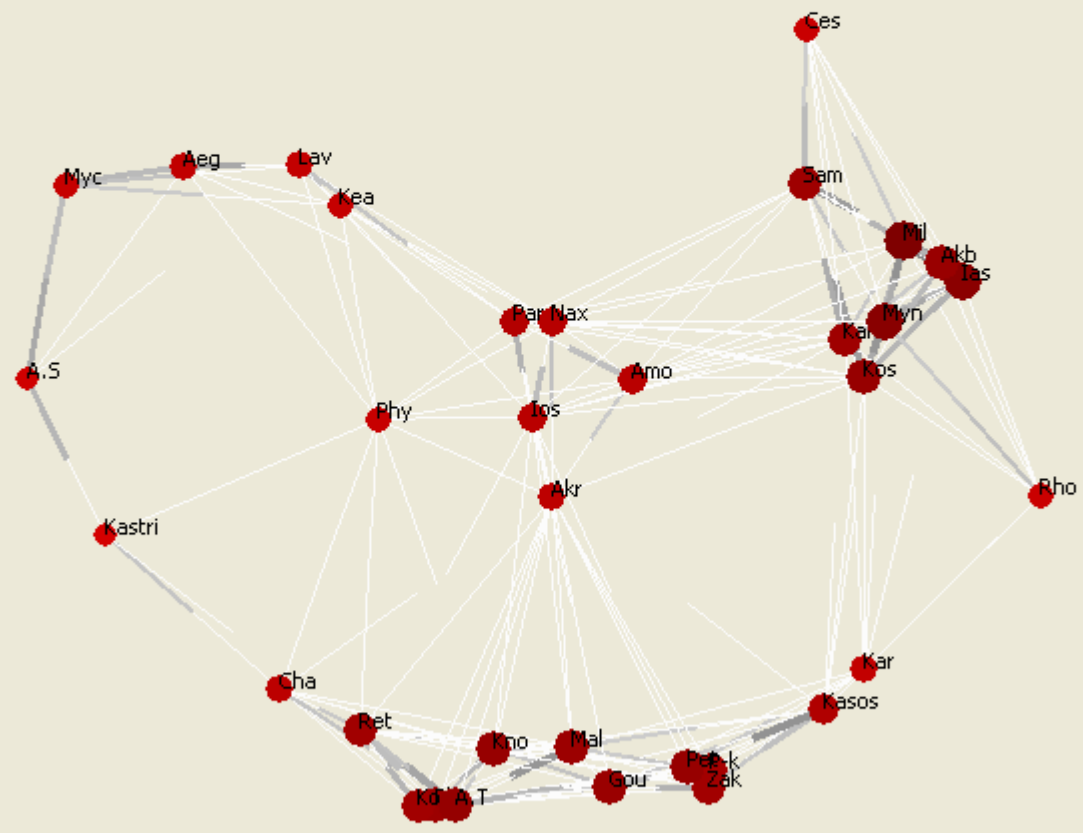
2.15

0.56

0.41

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m0.5j0.0k1.0b1.2s100.0Mcr4  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 0.5	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.01	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



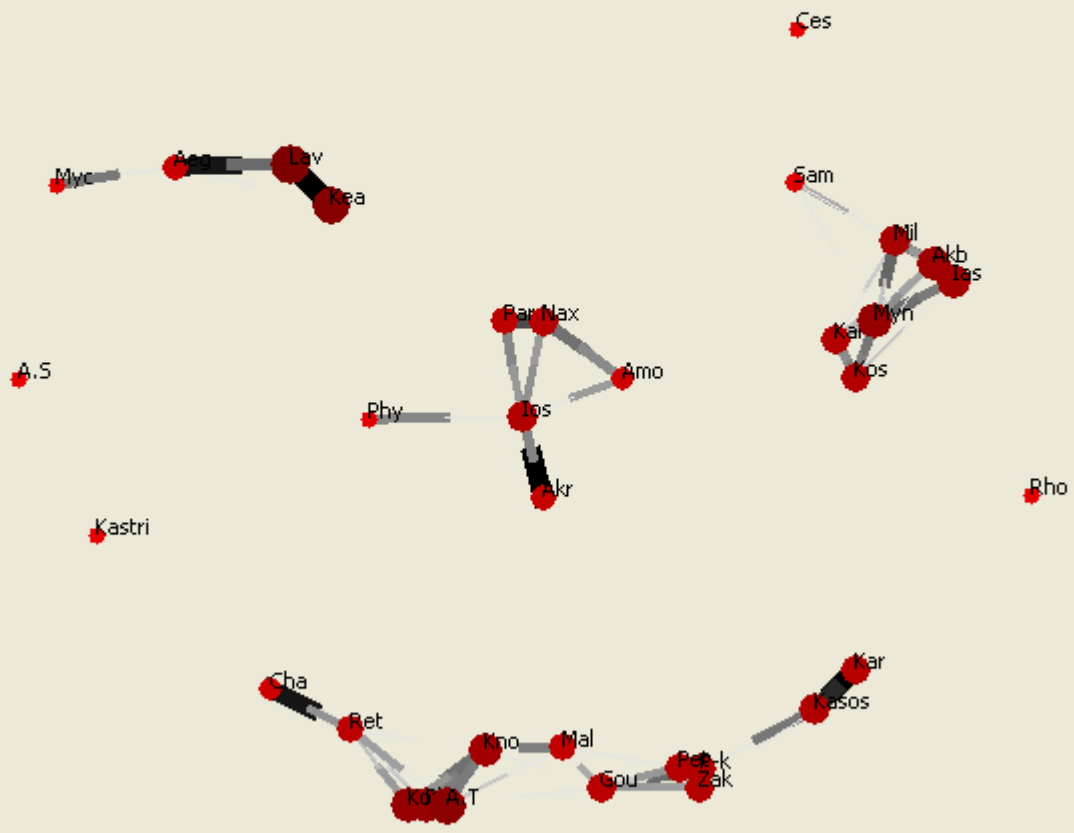
Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.44	0.39	0.75	2.24
Site Out W.Strength	1.44	0.39	0.74	2.24
Edge Weight	0.04	0.08	0.0	0.6
Edge Value	0.03	0.06	0.0	0.4

# Range of Distance Scales ( $d$ )

- Next 4 slides

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s50.0MCR0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 1.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 50.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.1	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	

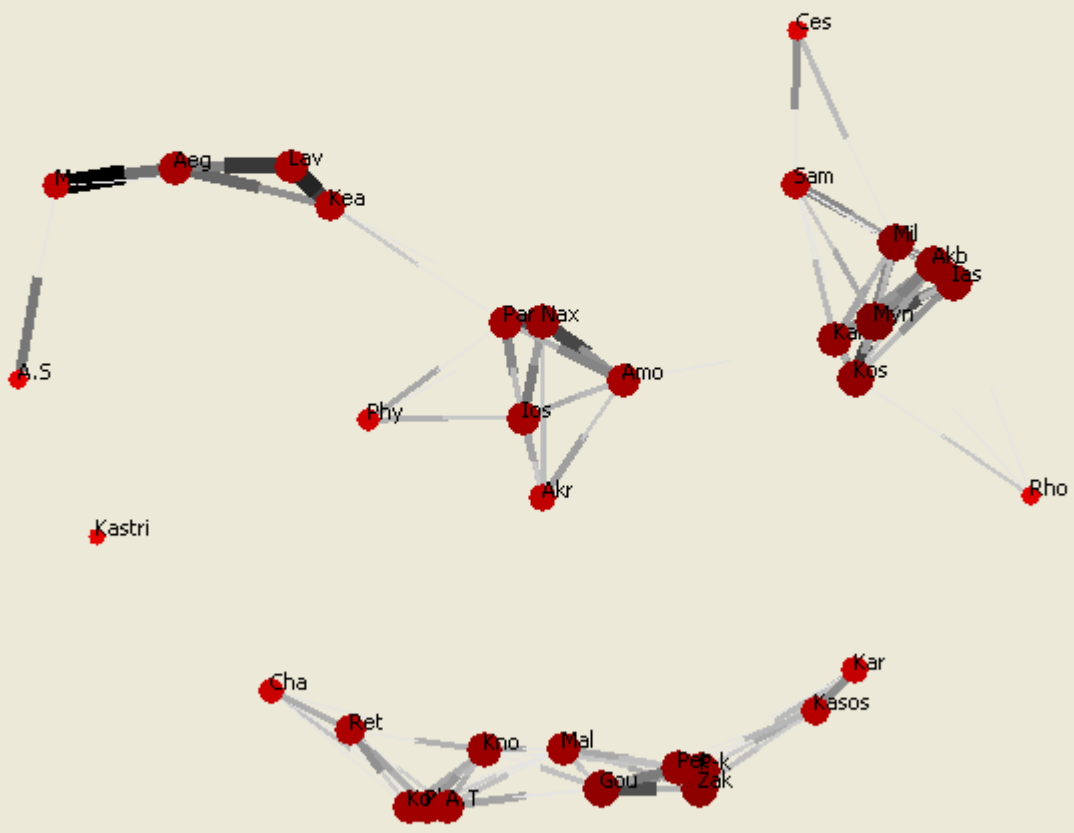


Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.38	0.57	0.48	2.52
Site Out W.Strength	1.32	0.65	0.07	2.5
Edge Weight	0.04	0.16	0.0	2.29
Edge Value	0.03	0.1	0.0	0.97



input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s75.0MCR0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

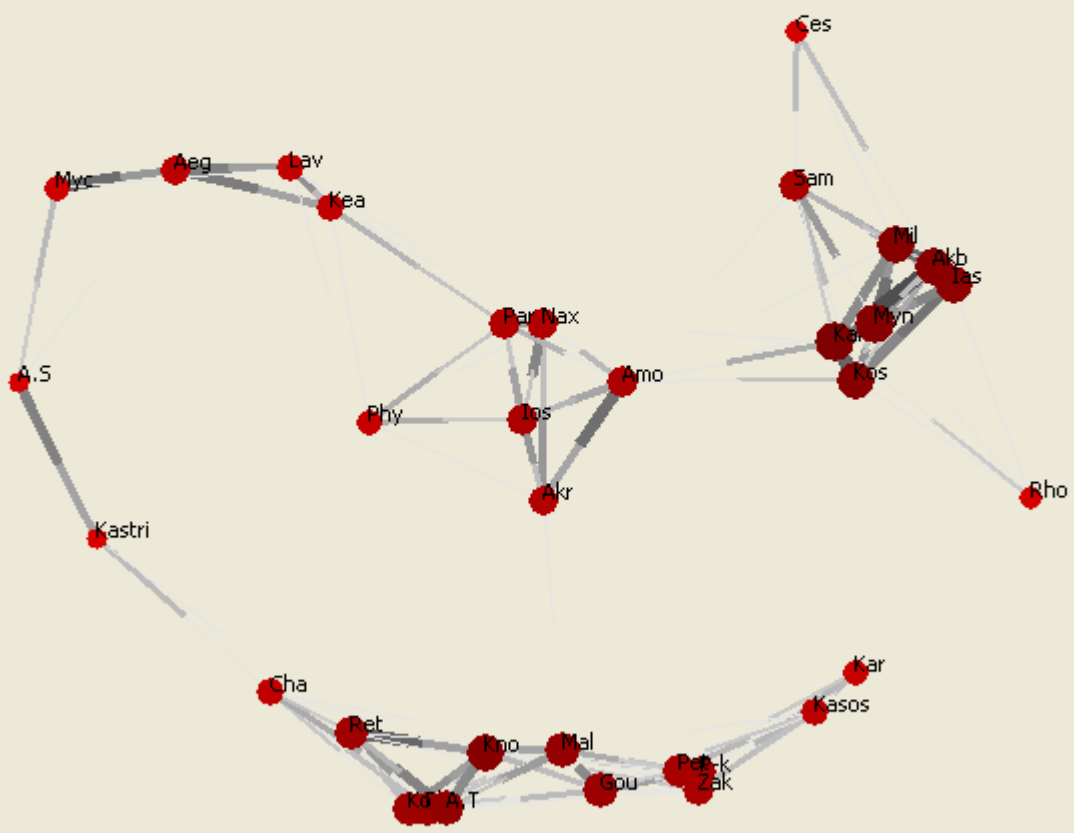
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 1.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 75.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.1	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.6	0.52	0.48	2.42
Site Out W.Strength	1.58	0.54	0.08	2.42
Edge Weight	0.05	0.13	0.0	1.03
Edge Value	0.03	0.08	0.0	0.96

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s100.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

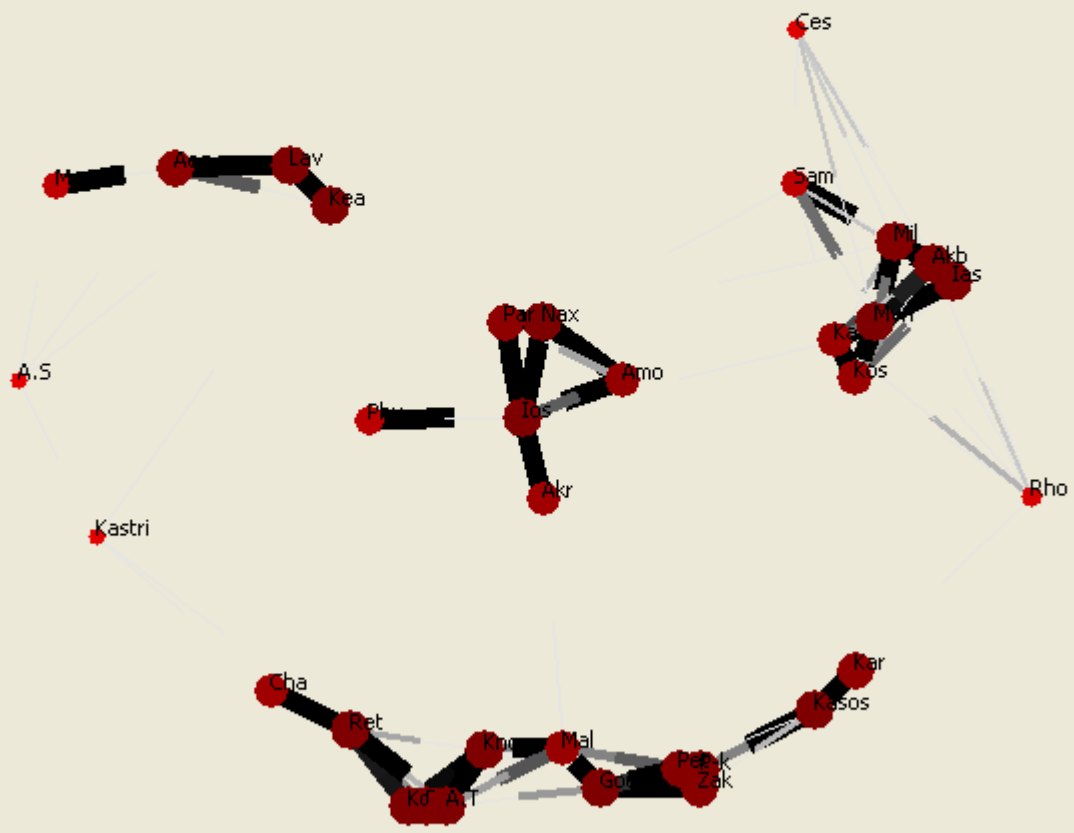
model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 1.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 100.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.1	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	1.78	0.56	0.82	2.74
Site Out W.Strength	1.78	0.56	0.82	2.74
Edge Weight	0.05	0.12	0.0	0.69
Edge Value	0.03	0.07	0.0	0.57

input file: aegean34  
 output files: output/aegean34\_v1\_3e-1.0m1.0j0.0k1.0b1.2s125.0Mcr0  
 Model: Standard Hamiltonian+Gravity (source and target site in trade term)

model number 1_3	Monte Carlo Update	Limits on Out Strength 1.0	max vertex value 5.0
mu 1.0	j 0.0	kappa 1.0	lambda 4.0
b 1.2	distance scale 125.0	short distance scale 5.0	metric number 5.0
beta 524288.0	Zero Colour Frac 0.1	Min. Colour Frac 0.2	Relative Vertex Display
Absolute Edge Display, Max 1.0	Influence Range 1.0 (prob=0.5)	sites by Size	



Quantity/Value	Average	Sigma	Minimum	Maximum
Site Weight	4.07	1.26	1.0	5.0
Site Out W.Strength	4.07	1.26	1.0	5.0
Edge Weight	0.12	0.43	0.0	4.82
Edge Value	0.03	0.1	0.0	0.96



# Network Description

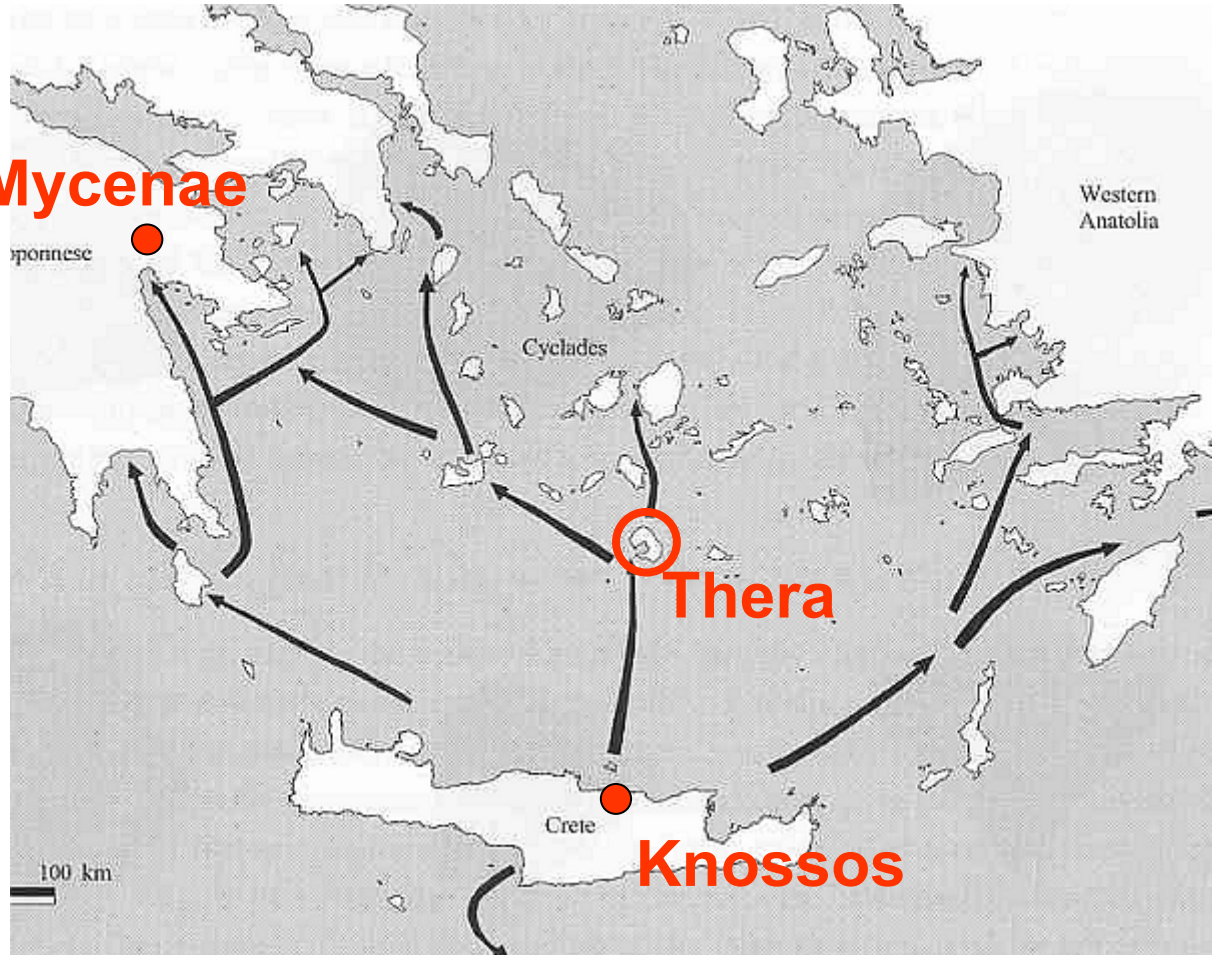


- $d_{ij}$  Fixed distance between sites identified from the archaeological record  
may be physical but may include penalties for prevailing winds, currents, land travel, ...
- $S_i$  Fixed site size = maximum local resources
- $v_i$  Variable site occupation fraction  
so if  $v_i > 1$  then site needs external resources  
» **Site Weight** ( $S_i v_i$ ) = Site '*population*'
- $e_{ij}$  Fractional Edge values  $0 \leq \sum_j e_{ij} \leq 1$   
» **Edge Weights** ( $S_i v_i e_{ij}$ )  
= '*Trade*' (interaction) going from site i to site j

# Robustness

- Are we finding a model that gives us the results we want?
  - Select on the basis of some pre-determined notion of reasonable results.
  - Do comparisons, do not use absolute results
- Do results depend on fine details of model?
  - Topological Congruence, Universality Classes
- Do results depend on how we encode the input data?
  - Scaling behaviour - when is an archaeological site a vertex?

# Middle Bronze Age Aegean (2000-1500 BC)



Palaces on Crete

‘Minoanisation’ begins

Theran eruption 1600 BC

‘Collapse’ – 1500 BC

DIFFERENT TO EBA  
of Broodbank (2000)

Ø Scale of networks

Ø Uneven site size

Ø Length of links

Ø Directionality

# Brief Chronology of the Aegean

Neolithic	7000 BC	•Initial colonisation – introduction of farming
	4000 BC	•Secondary colonisation of small islands
E B A	2500BC	•Nucleation and hierarchy in 3 <sup>rd</sup> millennium BC
	2200 BC	•Partial collapse?
M B A	1900BC	•Emergence of Minoan civilisation in 2 <sup>nd</sup> mill BC on Crete, sail technology appears
	1500BC	•Collapse
L	1450 BC	•Mycenaean mainlanders emerging power
B A	1200 BC	•Bronze Age collapse
	1100 BC	•‘Dark Ages’



# Efficiency?

- Need not be space filling in any sense.
- Need not be lowest number of links needed to connect all sites  
(Minimal Spanning Tree).
- ‘Deliberate Waste’ -  
may well favour redundancy to reduce path lengths, to increase possible interactions, to increase resilience to change.

# Site Strength

